

Cultural, Social and Technical Mathematics

Secondary IV

STUDY GUIDE



This Study Guide has been developed by teachers and consultants with the aim of helping students prepare for the MELS Uniform Examination in Secondary IV CST Mathematics. The production of this guide was possible through funding by an Anglophone community MELS Success Project.

Please note that this document is a "work in progress" and it will be reviewed during the 2014-2015 school year. Corrections and suggestions should be sent to your school board consultant.

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Table of Contents

Prepa	ring for the Exam and Exam Taking Strategies	
Prepa	ring a Memory Aid	1
Forma	at of the Uniform Exam	3
Skill Li	st	6
Quest	ions by Sections in the Visions Textbook	
	1.1 Points and Segments in the Cartesian Plane	9
	1.2 Lines in the Cartesian Plane	23
	1.3 Systems of Equations	41
	1.4 Half-Planes in the Cartesian Plane	51
	2.1 Diagrams and Statistics (Dispersion, Deviation, Stem and Leaf)	65
	2.2 Qualitative Interpretation of Correlation	81
	2.3 Quantitative Interpretation of Correlation	
	2.4 Interpretation of Linear Correlation	107
	3.1 Congruent Triangles	123
	3.2 Similar Triangles	137
	3.3 Metric Relations (Right Triangles)	151
	4.1 Real Functions	165
	4.2 Second-Degree Polynomial Function	179
	4.3 Exponential Function	193
	4.4 Step, Periodic and Piecewise Functions	209
	5.1 Trigonometric Ratios	223
	5.2 Finding Missing Measurements	237
	5.3 Calculating the Area of any Triangle	253
	6.2 Subjective Probability and Odds	267
	6.3 Mathematical Expectation	279

PREPARING FOR THE EXAM AND EXAM TAKING STRATEGIES

Preparing for the Exam

Preparation is key!

- Pay attention to hints your teacher gives you and take notes.
- Pay regular attention in class and ask for help when needed.
- Go to the tutorial sessions (review).
- Do not leave a topic misunderstood hoping it will not be on the exam. It will very likely be on the exam.
- Budget your time, schedule time to study so that you are well prepared for the test (weeks in advance). Do not wait until the day before!
- Create your own clear and well organized memory aid. This requires planning and time.
- Practice with questions from previous MELS Uniform Exams.
- Complete this booklet.
- Have a good night sleep the night before the exam. Go to bed earlier.
- Have a good breakfast. A healthy meal will give you the mental energy you will need to get through it.

The Day of the Exam

You will need to bring:

- at least two HB pencils and a good eraser
- a calculator (with or without graphic display) but make sure all data and programs are deleted
- a ruler
- your memory aid
- a watch to better pace yourself

Optional:

- a set square, a compass and a protractor
- additional graph paper

Exam Taking Strategies

- Keep a positive attitude and try to stay relaxed.
- When you first receive your test, do a quick read of the entire test in order to appropriately pace yourself. Look for what is easy and what will require more effort.
- Do the easiest problems first.
- Don't stay on a problem you are stuck on. Come back to it later.
- Read the entire question at least TWICE.
- Watch out for questions with expressions such as: NOT, STRONGEST TO WEAKEST, INCREASING, DECREASING, etc.
- Ask for clarifications, if needed.
- Write legibly and show all your work when required.
- Look over your test (review). Make sure you've answered everything.
- Do not leave any blanks.

PREPARING A MEMORY AID

A memory aid consists of one letter size (8 $\frac{1}{2}$ " x 11") sheet of paper IN <u>YOUR</u> HANDWRITING. BOTH sides may be used.

It should contain important information required for the exam. It should be NEAT and ORGANIZED. Have a plan and then write the elements on the sheet of paper. You might have to make more than one memory aid before being satisfied with the results. It's worth the time and effort.

Make sure to make your OWN memory aid. It is a good way to study for the exam and you will know where to find the items. You may not use someone else's memory aid (it is considered cheating). And besides, copying someone else's memory aid may not help you at all.

What can it contain?

- Formulas
- Example problems worked out
- The steps used in the problem listed in order
- Reminders of things to look out for in doing a problem
- Any rules used to solve problems
- Definitions
- Tips and hints

How can you organize it?

- The information should be organized by topic (e.g. triangles: congruent, similar...).
- Use lines (or boxes) to separate the different topics (e.g. a section for analytic geometry where you would include distance between two points, midpoint, slope, etc.).
- Use the resources your teacher suggests
- Make sure you include items you tend to forget.
- Use a color code system or a numbering system.

FORMAT OF THE UNIFORM EXAM

The exam will consist of 3 parts:

- A. Multiple Choice Questions (6 questions; 4 marks each)
- B. Short Answer Questions (4 questions; 4 marks each)
- C. Application Questions (6 questions; 10 marks each)

Part A. Multiple Choice Questions

You will read the questions from a Question Booklet and will choose a statement (A, B, C or D) that best represents your answer. You will answer on a machine-scored answer sheet by filling in a circle using an HB pencil. Make sure you fill it in completely.

In this section, you do not need to show work for marks. Always work out the problem entirely and check all the distractors. Do not stop reading when you think you found the right answer. Read everything. You will be given 4 marks or 0 for each question.

Do not leave a blank! Make a choice even if you don't know the answer! You have a 25% probability of getting it right.

Part B. Short Answer Questions

You will read the questions from a Question Booklet and will write a statement in the space provided in your Student Booklet.

In this section, you do not need to show work for marks. However, always work out the problem entirely anyways. You will be given 4 marks or 0 for each question. No part marks are given.

Do not leave a blank! Make an educated guess even if you don't know the answer!

Part C. Application Questions

You will read the questions from your Student Booklet and answer it in the Student Booklet (same booklet).

For each question, you must show all your work to justify your answer. Your work must be organized and clearly presented and cannot simply involve listing the calculator

applications used to obtain results or information.

You will be given a mark of 0 if you do not show work or if your work does not justify your answer (even if you have the correct answer).

You will be graded using the evaluation criteria for competency 2:

- Cr.1 Formulation of a conjecture suited to the situation, <u>if applicable</u>
- Cr.2 Correct use of appropriate mathematical concepts and processes
- Cr.3 Proper implementation of mathematical reasoning suited to the situation
- Cr.4 Proper organization of the steps in an appropriate procedure
- Cr.5 Correct justification of the steps in an appropriate procedure

The scoring will go as follows. The table on the right is for a conjecture situation. Most problems on the exam are scored according to the table on the left.

	Observable indicators corresponding to level						
	A B C D E						
Cr. 3	40	32	24	16	8	0	
Cr. 2	40	32	24	16	8	0	
Cr. 4	20	16	10	0	л	0	
Cr. 5	20	10	12	ð	4	U	

	Observable indicators corresponding to level					
	A B C D E					
Cr. 3	40	32	24	16	8	0
Cr. 2	20	16	12	8	4	0
Cr. 4	20	16	12	0	л	0
Cr. 5	20	10	12	0	4	0
Cr.1	20	16	12	8	4	0

As you can see, you can easily obtain marks for showing some work. Write down your process first (the steps) and then show all your work. At the very least, list the concepts you think apply, write out the applicable formulas, etc. Try something!

Do not leave a blank!

SKILL LIST

Can you do the following?

Put a check \checkmark in the appropriate box

Skill	Yes	Not yet
How to find the DISTANCE between two points		
How to find the MIDPOINT between two points		
How to find the point that divides a line into a given RATIO		
How to find the slope of a line		
How to express an equation in both STANDARD AND GENERAL FORM		
How to find the equation of a line given the slope and a point on the line		
How to find the equation of a line given two points on the line		
How to find the equation of a line parallel to a given line		
How to find the equation of a line perpendicular to a given line		
How to determine the number of solutions in a system (parallel, coincident)		
How to translate a story into a SYSTEM OF RELATIONS		
How to solve a system of equations using the COMPARISON METHOD		
How to display a system of relations and their solution on a graph		
How to solve a system of equations using the ELIMINATION METHOD		
How to solve a system of equations using the SUBSTITUTION METHOD		
How to recognize and translate an INEQUALITY		
How to solve an INEQUALITY graphically and check for feasible region		
How to determine and interpret the following properties in functions:		
What is a function		
The domain and range of a function		
Where the function is increasing, constant and decreasing		
The minimum and maximum		
The sign of a function		
The y-intercept of a function		
The zeros of a function (x-intercepts)		
How to work with the following functions (words, graph, equation, table):		
Zero degree		
First degree (direct)		
First degree (partial- positive and negative slopes)		
• 2^{nd} degree (quadratic) function $f(x) = ax^2$		
• Exponential function (growth and decay) $f(x) = ac^x$	1	1
Step function		t i i i i i i i i i i i i i i i i i i i
Periodic function		t i i i i i i i i i i i i i i i i i i i
Piecewise function	1	1

How to find an angle measure using TRIGONOMETRIC RATIOS (SIN, COS,	
How to find a side measure using TRIGONOMETRIC RATIOS (SIN, COS, TAN)	
How to find an angle or side measure using SINE LAW	
How to find the AREA OF A TRIANGLE - all three methods:	
General formula	
Hero's formula	
Trigonometric formula	
How to apply CLASSIFICATION OF TRIANGLES	
How to use PYTHAGOREAN THEOREM	
How to explain the differences in the properties of OUADRILATERALS	
How to find the areas of triangles/guadrilaterals/regular polygons	
How to determine the angle relationships when parallel lines are involved	
How to use algebra and angle relationships to solve for an unknown (x)	
How to prove that two triangles are congruent (SSS, SAS and ASA)	
How to prove that two triangles are similar (SSS, SAS and AA)	
How to find the unknown side lengths in similar figures	
How to find side lengths using METRIC RELATIONS	
How to read a FREQUENCY TABLE	
How to make and read a STEM AND LEAF PLOT	
How to calculate MEAN DEVIATION (and what it tells you about the data)	
How to calculate PERCENTILE RANK (and what it means)	
How to find a score of place GIVEN PERCENTILE RANK	
How to read a CONTINGENCY TABLE	
How to make and interpret a SCATTER PLOT	
How to estimate the CORRELATION COEFFICIENT (and what it means)	
How to determine the STRENGTH AND DIRECTION of the CORRELATION	
COEFFICIENT	
How to determine and represent the EQUATION OF A REGRESSION LINE	
(e.g. Median-Median method, Meyer line method, best fit method)	
How to draw a curve associated with the chosen model	
How to interpolate or extrapolate values using a REGRESSION LINE	
How to determine the PROBABILITY OF A SINGLE EVENT	
How to determine the PROBABILITY WITH WEIGHTED OUTCOMES	
How to switch back and forth between PROBABILITY AND ODDS	
How to determine ODDS FOR or ODDS AGAINST	
How to CALCULATE MATHEMATICAL EXPECTATION IN GAMES OF CHANCE	
How to MAKE A GAME FAIR using Mathematical expectation	
How to recognize and associate the type of probability to a situation:	
EXPERIMENTAL, THEORETICAL and SUBJECTIVE	

1.1 Points and Segments in the Cartesian Plane

Question:

What is the rate of change for line segment AB?



General Strategies:

- 1. Read the question.
- 2. Highlight key words.
- Identify the math topic.
- 4. Re-read the question.
- 5. Refer to your memory aid, as needed.
- Solve the problem without looking at choices shown (A, B, C and D).
- 7. Look at all the choices.
- 8. Match your answer to the appropriate choice.

Do not leave a blank! Make a choice!

My Strategies:



Explore Learning Gizmos, http://www.explorelearning.com/ look up: Slope

Question:	General Strategies:
What is the endpoint of a line segment which has one end at (6, 18) and the midpoint at (18, 30)?	 Read the question. Highlight key words. Identify the math
A) (-6, 6)	topic.
B) (12, 24)	 Refer to your memory aid as peeded
C) (24, 12)	6. Solve the problemwithout looking at
D) (30, 42)	 without looking at choices shown (A, B, C and D). 7. Look at all the choices. 8. Match your answer to the appropriate choice. Do not leave a blank! Make a choice! My Strategies:



Quest	tion:	General Strategies:			
Point P is located $\frac{3}{5}$ of the distance from point B (25, 75) and point A (10, 30).		 Read the question. Highlight key words. Identify the math 			
Which	coordinates represent point P?	4.	topic. Re-read the		
A)	(15.625, 46.875)	5.	question. Refer to your		
B)	(16, 48)		memory aid, as needed.		
C)	(19, 57)	6.	Solve the problem without looking at		
D)	(19.375, 58.125)	7. 8. Do r Mał	choices shown (A, B, C and D). Look at all the choices. Match your answer to the appropriate choice. not leave a blank! & a choice! Strategies:		



Khan Academy video: http://www.khanacademy.org/math/algebra/linear-equations-andinequalitie/more-analytic-geometry/e/midpoint formula

Suggested Strategies:

Page 15

Question:	General Strategies:
On a coordinate plane, Jim's house is situated on a line that runs from his school to the swimming pool.	 Read the question. Highlight key words. Identify the math topic
B (1200, 1600).	 4. Re-read the question. 5. Make a prediction
Jim's house divides line segment AB into a ratio of 4:1 from point A. What are the coordinates of Jim's house?	about the answer- what will it look like? (an equation, a
	number, etc.). 6. Refer to your memory aid, as needed.
	 Solve. Ask yourself whether your answer makes
	sense. 9. Write your answer. Do not leave a blank!
	My Strategies:
Jim's house is situated at (,).	

Answer and Solution:	Suggested Strategies:				
Division point formula: $ \begin{pmatrix} x_p, y_p \\ = \\ $	Notice the keywords to see what kind of problem it is: Line, point Divides Ratio Coordinates				
$x_{p} = 200 + \frac{4}{5}(1200 - 200)$ $x_{p} = 200 + \frac{4}{5}(1000)$ $x_{p} = 200 + 800$ $x_{p} = 1000$ $y_{p} = 800 + \frac{4}{5}(1600 - 800)$ $y_{p} = 800 + \frac{4}{5}(800)$ $y_{p} = 800 + 640$ $y_{p} = 1440$	This is a division point question. Determine whether the ratio given is part to part or part to whole. In this case it is part to part – which means you'll add the numbers to create the fraction in the formula. Pay attention to the end from which the ratio is being measured – in this case from point A. It always helps to make a sketch of the situation.				
Jim's house is situated at (1000, 1440).					
Additional Resources:					
Visions Volume 1, Section 1.1, p. 16 (Point of Division) Khan Academy video: <u>http://www.khanacademy.org/math/algebra/linear-equations-and-</u> inequalitie/more-analytic-geometry/e/midpoint_formula					



QUESTION 5

Answer and Solution:	Suggested Strategies:			
$d(A, C) = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$ A (-30,40) & C (20, 58) $d(A, C) = \sqrt{(20 - (-30))^2 + (58 - 40)^2}$ $d(A, C) = \sqrt{2500 + 324}$ $d(A, C) = \sqrt{2500 + 324}$ $d(A, C) = \sqrt{2824}$ $d(A, C) \approx 53.1413 \text{ m}$ B (90,35) & C (20, 58) $d(B, C) = \sqrt{(20 - 90)^2 + (58 - 35)^2}$ $d(B, C) = \sqrt{(-70)^2 + (23)^2}$ $d(B, C) = \sqrt{4900 + 529}$ $d(B, C) = \sqrt{5429}$ $d(B, C) \approx 73.6817 \text{ m}$ $73.6817 - 53.1413 = 20.5404$	The key word here is "longer" which implies length. And with the Cartesian plane (coordinates) as part of the question we'll want to use the distance formula. Determine the distances we need: AC and BC (we don't need AB). And then subtract to find the difference between the two distances calculated.			
\overline{BC} is 20.54 m longer than \overline{AC} .				
Additional Resources:				
Visions Volume 1, Section 1.1, p. 15 (Distance between Two Points) Khan Academy video: <u>http://www.khanacademy.org/math/algebra/linear-equations-and-</u> <u>inequalitie/more-analytic-geometry/v/midpoint-formula</u>				

QUESTION 6

Question:

Bill says that his house is exactly the same distance to the water tower as Alan's house is.

Alan does not believe him so he makes a Cartesian plane and puts all the information that he knows is true on the graph.

He starts by making Birch St. the x-axis and Maple Ave. the y-axis since they are perpendicular to each other.

He knows his house is in a straight line with Bill's and the school is midway on the line between their houses.

He also knows that the water tower is on Maple Ave. 1100 m from Birch St.

Finally he puts the co-ordinates of his house (-400, 200) and the coordinates of the school (200, 400) on the graph.

Which of the boys is correct?



General Strategies:

- 1. Read the problem.
- 2. Highlight key words.
- Identify the math topics.
- 4. Re-read the problem.
- Define your steps (your game plan) – this is criteria 3.
- 6. Refer to your memory aid, as needed.
- 7. Solve.
- If you get stuck on a calculation, pick a number and keep going.
- 9. Ask yourself whether your answer makes sense.
- Write your answer statement.
 Show any or all your work! Do not leave a

blank page!

My Strategies:

Answer and Solution:	Suggested Strategies:	
Distance between Bill's house and the water tower:	Begin by transferring information from the text	
Bill's house: (-400, 200) Water tower: (0, 1100)	onto the diagram.	
$d = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$ $d = \sqrt{(0400)^2 + (1100 - 200)^2}$ $d = \sqrt{(400)^2 + (900)^2}$ $d = \sqrt{160000 + 810000}$ $d = \sqrt{970000}$ $d \approx 984.88$ Coordinates of Alan's house: Bill's house: (-400, 200) School: (200, 400), the midpoint $\frac{x_1 + x_2}{2} = x_m \qquad \frac{y_1 + y_2}{2} = y_m$ $\frac{-400 + x_2}{2} = 200 \qquad \frac{200 + y_2}{2} = 400$	To answer this question you have to calculate the distance between each of the houses and the water tower. For that, you need the three sets of coordinates; Bill's house, Alan's house and the water tower. You are given the coordinates of the water tower (0, 1100) and Bill's house (-400, 200).	
$-400 + x_2 = 400 \qquad 200 + y_2 = 800$ $x_2 = 800 \qquad y_2 = 600$	Using the coordinates of Bill's house and the school, you can determine	
Alan's house: (800, 600)	the coordinates of Alan's house.	
$d = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$ $d = \sqrt{(0 - 800)^2 + (1100 - 600)^2}$ $d = \sqrt{(-800)^2 + (500)^2}$ $d = \sqrt{640000 + 250000}$ $d = \sqrt{890000}$ $d \approx 943.40$		
Alan is correct; their houses are not same distance from the water tower.		
Additional Resources:		
Visions Volume 1, Section 1.1, pp. 15-16 Khan Academy video: <u>http://www.khanacademy.org/math/algebra/linear-equations-and-</u>		

inequalitie/more-analytic-geometry/v/midpoint-formula

1.2 Lines in the Cartesian Plane

Question:

What is the rule for the linear function that corresponds to the table below?

x	-10.2	-6.4	3.4	12.8
У	53.7	40.4	6.1	-26.8

- A) -7x 2y 36 = 0
- B) 7x 2y + 36 = 0
- C) -7x + 2y 36 = 0
- D) 7x + 2y 36 = 0

General Strategies:

- 1. Read the question.
- Highlight key words.
 Identify the math
- topic. 4. Re-read the
 - question.
- 5. Refer to your memory aid, as needed.
- Solve the problem without looking at choices shown (A, B, C and D).
- 7. Look at all the choices.
- 8. Match your answer to the appropriate choice.

Do not leave a blank! Make a choice!

My Strategies:

Answer and Solution:	Su	ggested Strategies:
Formula for a linear equation: $y = ax + b$ <u>Coordinates used to find the rule:</u> (-10.2, 53.7) (-6.4, 40.4)	I) II)	Recognize the table of values is a series of coordinates you need two sets to find the rule. Choose any coordinate pair and label them x_1 ,
slope (a) = $\frac{y_2 - y_1}{x_2 - x_1}$ slope (a) = $\frac{40.4 - 53.7}{-6.4 - (-10.2)} = \frac{-13.3}{3.8} = -3.5$	111)	y_1 and x_2 , y_2 Find the rate of change between these coordinate pairs using the formula: $slope = \frac{y_2 - y_1}{x_1 - x_2}$
y = ax + b y = -3.5x + b 40.4 = -3.5(-6.4) + b	IV)	x_2-x_1 Plug the rate of change into the formula $y = ax + b$
40.4 = 22.4 + b 18 = b y = -3.5x + 18	V)	Substitute any of the (x, y) coordinate pairs from the table into the equation and solve for the initial value (b)
Convert slope from decimal form to fraction form and multiply each term by the denominator $y = \frac{-7}{2}x + 18$ $2y = -7x + 36$ $2y + 7x - 36 = 0$ $7x + 2y - 36 = 0$	∨ I)	If your rate of change or initial value is in fraction form, multiply each term by the LCM (least common multiple) of the two denominators)Keeping in mind the signs, move all of the terms to one side of the equal sign.
The answer is D.		
Additional Resources:		

Visions Volume 1, Section 1.2, p. 26 (Equation of Line from Slope and Intercepts) Khan Academy video: <u>http://www.khanacademy.org/math/algebra/linear-equations-and-inequalitie/more-analytic-geometry/v/algebra--slope-and-y-intercept-intuition</u> Explore Learning Gizmos, <u>http://www.explorelearning.com/</u> look up:

- Point-Slope Form of a Line
- Slope-Intercept Form of a Line

Question:	General Strategies:
Which of the following equations represents a line perpendicular to $4x + 3y + 12 = 0$?	 Read the question. Highlight key words. Identify the math
A) $3x + 4y - 8 = 0$	topic. 4. Re-read the
$B) \qquad y = \frac{4}{3}x - 4$	question. 5. Refer to your
C) $-3x + 4y - 8 = 0$	memory aid, as needed.
D) $y = -\frac{4}{3}x + 4$	 6. Solve the problem without looking at choices shown (A, B, C and D). 7. Look at all the choices. 8. Match your answer to the appropriate choice. Do not leave a blank! Make a choice! My Strategies:

Answer and Solution: Suggested Strategies: The word *perpendicular* Find the slope of 4x + 3y + 12 = 01) in this problem should immediately cause you 3v = -4x - 12 $\frac{3y}{3} = \frac{-4x - 12}{3}$ to write the negative reciprocal rule for perpendicular slopes: $y = \frac{-4}{3}x - 4$ the slope is $\frac{-4}{3}$ $\frac{a}{b} \rightarrow \frac{-b}{a}$ Find the perpendicular slope: $\frac{a}{b} \rightarrow \frac{-b}{a}$ II) Start by converting the equation from 'general' The perpendicular slope is $\frac{3}{4}$ (options B and D are 'out') form to 'slopeintercept' form in order to get a better look at Convert options A and C to slope-intercept form and compare slopes. the slope. Option A III) Find the negative 3x + 4y - 8 = 0reciprocal of the slope 4y = -3x + 8from the equation $\frac{4y}{4} = \frac{-3x+8}{4}$, given in the problem. This is the slope we are looking for in our The slope is not $\frac{3}{4}$, option A is wrong. multiple-choice answers. IV) Remember that we Option C only care about finding -3x + 4y - 8 = 0a perpendicular line in 4y = 3x + 8this problem, so we only need to worry $\frac{4y}{4} = \frac{3x+8}{4}$ about the slopes. Ignore the initial values altogether... they are The slope is equal to $\frac{3}{4}$, option C is correct. only distractors here. The answer is C. **Additional Resources:**

Visions Volume 1, Section 1.2, p. 27 (Perpendicular Line) Khan Academy video: <u>http://www.khanacademy.org/math/algebra/linear-equations-and-inequalitie/more-analytic-geometry/e/line_relationships</u> Г

Que	stion:	General Strategies:
Wha	t is the <i>x</i> -intercept for the following linear equation: 2x + 3y + -6 = 0	 Read the question. Highlight key words. Identify the math
A) B)	3 2	 topic. Re-read the question. Refer to your memory aid, as needed.
C)	2	 Solve the problem <u>without looking</u> at choices shown (A, B,
נט	3	C and D). 7. Look at all the choices. 8. Match your answer to the appropriate choice. Do not leave a blank! Make a choice!
		My Strategies:

Answer and Solution:	Su	ggested Strategies:
Set the 'y' value to 0 and solve for x. 2x + 0 + 6 = 0 2x + 6 = 0 2x = 6	1)	Remember that the x-intercept is the point on a graph where the line crosses the x-axis (y = 0)
$x = \frac{-6}{2}$ $x = -3$	11)	Set y = 0 and solve for x.
Set the 'y' value to 0 and solve for x.		
$0 = \frac{-2}{3}x - 2$ $2 = \frac{-2}{3}x$ $2\left(\frac{3}{-2}\right) = x$ -3 = x		
The answer is A.		
Additional Resources:		
Visions Volume 1, Section 1.2, p. 26 (Equation of a Line) Khan Academy video: <u>http://www.khanacademy.org/math/algebra/linear-equations-and- inequalitie/more-analytic-geometry/v/algebraequation-of-a-line</u>		

Question:

Which rule represents the line parallel to 3x - 4y - 24 = 0 that passes through point P(-8, 7)?

A)
$$-3x + 4y - 13 = 0$$

B)
$$-3x + 4y - 52 = 0$$

C)
$$y = \frac{3x}{4} + 52$$

D)
$$3y = -4x - 13$$

General Strategies:

- 1. Read the question.
- 2. Highlight key words.
- Identify the math topic.
- 4. Re-read the question.
- 5. Refer to your memory aid, as needed.
- Solve the problem without looking at choices shown (A, B, C and D).
- 7. Look at all the choices.
- 8. Match your answer to the appropriate choice.

Do not leave a blank! Make a choice!

My Strategies:
Answer and Solution:	Su	ggested Strategies:
Convert the equation from general form to <i>y</i> -intercept form 3x - 4y - 24 = 0	I)	Remember that parallel lines always have the same slope.
-4y = -3x + 24 $\frac{-4y}{-4} = \frac{-3x + 24}{-4}$ $y = \frac{3x}{4} - 6$, the slope of the parallel line must be $\frac{3}{4}$ y = ax + b $y = \frac{3}{4}x + b$	11)	Convert the rule in the question from 'general' form to 'slope-intercept' form in order to find the slope. This slope will be the same in your new parallel line.
7 = 0.75(-8) + b 7 = -6 + b 13 = b	III)	Plug the parallel slope (a) into the formula y = ax + b
$y = \frac{3}{4}x + 13$ Convert the rule from slope-intercept form to general form by	I∨)	Substitute the coordinates of point P (-8, 7) into the new equation and solve for the initial value
multiplying by the denominator 3		(<i>b</i>).
$(4)y = (4)\frac{1}{4}x + (4)13$ 4y = 3x + 52 4y - 3x - 52 = 0	∨)	Convert your answer from slope-intercept form to general form and look for a match.
-3x + 4y - 52 = 0, The answer is B.	VI)	You can also convert the rules from general form into slope-intercept form in the multiple choice section.
Additional Resources:		

Visions Volume 1, Section 1.2, p. 27 (Parallel Line) Khan Academy video: <u>http://www.khanacademy.org/math/algebra/linear-equations-and-inequalitie/more-analytic-geometry/v/parallel-line-equation</u>

Line L has equation -4x + 5y - 10 = 0.

What is the *x*-intercept of the line perpendicular to L that passes through point P (12, 15)?

General Strategies:

- 1. Read the question.
- 2. Highlight key words.
 3. Identify the math
- topic. 4. Re-read the
- question.
 5. Make a prediction about the answerwhat will it look like? (an equation, a number, etc.).
- Refer to your memory aid, as needed.
- 7. Solve.
- Ask yourself whether your answer makes sense.

9. Write your answer. Do not leave a blank!

My Strategies:

The *x*-intercept of the line perpendicular to L that passes through P is

Answer and Solution: Suggested Strategies: I) Remember that an x-Convert the equation from general form to y-intercept intercept is the point at which a line crosses the -4x + 5y - 10 = 0*x*-axis. The *y*-value of this 5v = 4x + 10coordinate must be $\frac{5y}{5} = \frac{4x + 10}{5}$ equal to 0 (y = 0) at this point. II) Start by converting the $y = \frac{4x}{5} + 2$, the slope of the line is $\frac{4}{5}$ equation from 'general' form to 'slope-intercept' form in order to get a Find the perpendicular slope: better look at the slope. $\frac{a}{b} \rightarrow \frac{-b}{a}, \frac{4}{5} \rightarrow \frac{-5}{4}$, the perpendicular slope is $\frac{-5}{4}$ III) The word *perpendicular* in this problem should y = ax + bimmediately cause you to write the negative $y = \frac{-5}{4}x + b$ reciprocal rule for perpendicular slopes: 15 = -1.2(12) + b $\frac{a}{b} \rightarrow \frac{-b}{a}$ 15 = -14.4 + bIV) Since we are looking for 30 = bthe line that is perpendicular to $y = \frac{-5}{4}x + 30$ -4x + 5y - 10, we'll need the negative reciprocal $\left(\frac{-b}{a}\right)$ of the slope from the equation given in the Set the 'y' value to 0 and solve for x. problem. V) Use the perpendicular $0 = \frac{-5}{4}x + 30$ slope in a new y = ax + b' rule. VI) Substitute the $-30 = \frac{-5}{4}x$ coordinates of point P (12, 15) into the new $-30\left(\frac{4}{-5}\right) = x$ equation and solve for the initial value (b). VII) Once you've got your 24 = xrule for the perpendicular line The x-intercept of the line perpendicular to L that passes through P finished, find the xis (24, 0). intercept by making y = 0 and solving for x. **Additional Resources:**

Visions Volume 1, Section 1.2, pp. 26-27 Khan Academy video: <u>http://www.khanacademy.org/math/algebra/linear-equations-and-inequalitie/more-analytic-geometry/v/parallel-line-equation</u>

The slope of line 1 is $\frac{4}{3}$ with a *y*-intercept of -3.

Line 2 is perpendicular to line 1 and passes through point (2, 5).

What is the equation of line 2?

General Strategies:

- 1. Read the question.
- 2. Highlight key words.
- Identify the math topic.
- 4. Re-read the question.
- Make a prediction about the answerwhat will it look like? (an equation, a number, etc.).
- 6. Refer to your memory aid, as needed.
- 7. Solve.
- 8. Ask yourself whether your answer makes sense.
- 9. Write your answer. Do not leave a blank!

My Strategies:

The equation of line 2 is _____

Answer and Solution:	Suggested Strategies:		
$y = \frac{-3x}{4} + 6.5$	 Use the negative reciprocal of the slope of line 1 to find the slope of 		
Line 1 :	line 2.		
$y = \frac{4x}{3} - 3$	 Use the function form of the equation, y = ax + b, with point 		
Line 2 :	(2, 5) and the new slope.		
$a = \frac{-3}{4}$			
Substitute point (2, 5) in for the x and y to solve for "b".			
$y = \frac{-3x}{4} + b$			
$y = \frac{-3(2)}{4} + b$			
$5 = \frac{-6}{4} + b$			
$b = 5 + \frac{3}{2} = 6.5$			
$y = \frac{-3x}{4} + 6.5$			
The equation of line 2 is $y = \frac{-3x}{4} + 6.5$			
Additional Resources:			
Visions Volume 1, p. 27 (Mathematical Knowledge Summary) Khan Academy video: <u>http://www.khanacademy.org/math/algebra/systems-of-eq-and-ineq/fast-</u>			

systems-of-equations/v/solving-systems-of-equations-by-elimination Explore Learning Gizmos, <u>http://www.explorelearning.com/</u> look up: Systems of Linear Equations

Question:	General Strategies:
Given the equation: 8x + 6y + 12 = 0	 Read the question. Highlight key words. Identify the math topic.
 A) What is the <i>x</i>-intercept? B) What is the <i>y</i>-intercept? 	 4. Re-read the question. 5. Make a prediction about the answer-what will it look like? (an equation, a number, etc.). 6. Refer to your memory aid, as needed. 7. Solve. 8. Ask yourself whether your answer makes sense. 9. Write your answer. Do not leave a blank! My Strategies:
The <i>x</i> -intercept is	
The <i>y</i> -intercept is	

Answer and Solution:

Algebraically:

у

х

х

A) x-intercept

$$y = 0$$

 $8x + 6y + 12 = 0$
 $8x + 6(0) + 12 = 0$
 $8x = -12$
 $x = -\frac{12}{8} = \frac{-3}{2}$
 $x = -\frac{3}{2}$
B) y-intercept
 $x = 0$
 $8(0) + 6y + 12 = 0$
 $6y = -12$
 $y = -\frac{12}{6} = -2$
 $y = -2$

Graphically:



The x-intercept is $-\frac{3}{2}$.

The y-intercept is -2.

Additional Resources:

Visions Volume 1, p. 26 (Mathematical Knowledge Summary) Explore Learning Gizmos, http://www.explorelearning.com/ look up:

Suggested Strategies:

When finding the intercepts, the other coordinate is 0:

x-intercept means y = 0y-intercept means x = 0.

You can also solve this question graphically by changing the equation into function form and plotting the y-intercept and slope.

A car is travelling along a straight path from point A (-24, -39) to point B (30, 33).

The car breaks down, having completed exactly two-thirds of the trip.

A tow truck must travel along a path that is perpendicular to the car's path, leaving from a garage located somewhere along the x-axis.

How far must the tow-truck travel to get from the garage to the car? (All units are in km.)



General Strategies:

- 1. Read the problem.
- 2. Highlight key words.
- Identify the math topics.
- 4. Re-read the problem.
- Define your steps (your game plan) – this is criteria 3.
- 6. Refer to your memory aid, as needed.
- 7. Solve.
- If you get stuck on a calculation, pick a number and keep going.
- 9. Ask yourself whether your answer makes sense.
- Write your answer statement.
 Show any or all your work! Do not leave a

My Strategies:

blank page!

Answer and Solution:

Find the coordinates of the point where the car breaks down

Division point 2/3 of the way between A and B Division point : $(x_1 + \frac{a}{b}(x_2 - x_1), y_1 + \frac{a}{b}(y_2 - y_1))$ A (-24, -39) B (30, 33) $(-24 + \frac{2}{3}(30 - (-24)), -39 + \frac{2}{3}(33 - (-39)))$ $(-24 + \frac{2}{3}(54), -39 + \frac{2}{3}(72))$ Call the position of the car point C

C (12.9)

Find the slope of the rule for the line the car travels

Formula for a linear equation: y = ax + bCoordinates used to find the rule: A (-24,-39) B (30, 33) $slope(a) = \frac{y_2 - y_1}{x_2 - x_1}$

slope (*a*) =
$$\frac{33 - (-39)}{30 - (-24)} = \frac{72}{54} = \frac{4}{3}$$

Find the equation for the tow-truck's path

The tow-truck's path will be perpendicular (negative reciprocal slope) and passes through point C (12, 9), *the car* $\frac{a}{b} \rightarrow \frac{-b}{a}, \frac{4}{3} \rightarrow \frac{-3}{4}, \text{ the tow-truck's slope is } \frac{-3}{4}$

y = ax + b, passing through (12, 9)

$$y = -\frac{3}{4}x + b$$

$$9 = \frac{-3}{4}(12) + b$$

$$9 = -9 + b$$

$$18 = b$$

Suggested Strategies:

- Recognize that the question is asking for a distance between two points, the car and the garage. This problem requires us to first find and then use those coordinates.
- II) Start by using the division point formula to find the coordinates of the car when it breaks down.
- III) Then find the coordinates of the garage,
 - we know that it is on the x-axis (so the y-coordinate is = 0)
 - b. We know that it is on the path that is perpendicular to AB
- IV) Find the slope of AB so we can use its negative reciprocal to define the slope of the line between the car and the garage.
- V) Plug the (x, y) coordinates of the car into the formula for the tow-truck's path, then solve for the initial value to complete the equation for the towtruck's path.

$$y = \frac{-3}{4}x + 18$$
(V) Using the equation of
the line for the tow-
truck's parage is on the *x*-
axis) and solve for *x*.
Set the 'y' value to 0 and solve for *x*.

$$y = \frac{-3}{4}x + 18$$

$$0 = \frac{-3}{4}x + 18$$

$$-18 = \frac{-3}{4}$$

$$-18 (\frac{4}{-3}) = x$$

$$24 = x$$
The coordinates of the garage are: (24, 0)
Find the distance from the garage to the car.
Garage (24, 0)
Car (12, 9)

$$distance = \sqrt{(12 - 24)^2 + (9 - 0)^2}$$

$$distance = \sqrt{(12 - 24)^2 + (9 - 0)^2}$$

$$distance = \sqrt{(14 + 81)}$$

$$distance = 15$$
Final answer: the distance the tow-truck must travel from the garage
to the car is 15 km.
Additional Resources:
Visions Volume 1, Section 1.2, pp. 26-27
Visions Volume 1, Section 1.1, pp. 15-16

1.3 Systems of Equations

Consider the following system of linear equations.

$$2x + 3y + 6 = 0$$

$$y = \frac{-2x}{3} - 4$$

Which of the following statements is true?

- A) The system has an infinite number of solutions.
- B) The system has a unique solution.
- C) The system has no solution.
- D) The system has two solutions.

General Strategies:

- 1. Read the question.
- 2. Highlight key words.
 3. Identify the math topic.
- 4. Re-read the question.
- 5. Refer to your memory aid, as needed.
- Solve the problem <u>without looking</u> at choices shown (A, B, C and D).
- 7. Look at all the choices.
- 8. Match your answer to the appropriate choice.

Do not leave a blank! Make a choice!

My Strategies:

Answer and Solution:	Suggested Strategies:	
Answer and Solution: $2x + 3y + 6 = 0$ $y = -2x - 4$ 3 $2x + 3(-2x - 4) + 6 = 0$ $2x + -2x - 12 + 6 = 0$ $2x - 2x - 6 = 0$ $0 \neq 6$ Since the left side does not equal the right side there is no possible solution; if graphed you would see that the lines are parallel and never intersect. ALTERNATE METHOD	 Suggested Strategies: Solve the system. Check to see if the slopes are the same; If not, there will be one solution; If the slopes are the same, check to see if the <i>y</i>-intercepts are the same If they are the same, there is an infinite number of solutions since 	
2x + 3y + 6 = 0 $y = \frac{-2x}{3} - 4$ 2x + 3y + 6 = 0 3y = -2x - 6 $y = \frac{-2x - 6}{3}$ $y = \frac{-2x}{3} - 2$ The slopes (<i>a</i>) are the same and the <i>y</i> -intercepts (<i>b</i>) are different; if graphed you would see that the lines are parallel and never intersect.	solutions since they are the same line; If they are not, they are parallel lines and the system has no solution.	
The answer is C.		
Additional Resources: Visions Volume 1, p. 40 (Mathematical Knowledge Summary) Khan Academy video: <u>http://www.khanacademy.org/math/algebra/systems-of-eq-and-ineq/fast-systems-of-equations/v/solving-systems-of-equations-by-elimination</u> Explore Learning Gizmos, <u>http://www.explorelearning.com/</u> look up: Systems of Linear Equations		

Given the following system of equations.

$$2x - 5y + 12 = 0$$

$$x - 3y = 4$$

What is the solution for this system?

- A) (-41, -14)
- B) (-44, -20)
- C) (-56, -20)
- D) (-56, -12)

General Strategies:

- Read the question.
 Highlight key words.
- Identify the math topic.
- 4. Re-read the question.
- 5. Refer to your memory aid, as needed.
- Solve the problem <u>without looking</u> at choices shown (A, B, C and D).
- 7. Look at all the choices.
- 8. Match your answer to the appropriate choice.

Do not leave a blank! Make a choice!

My Strategies:

Answer and Solution:	Suggested Strategies:
2x - 5y + 12 = 0 x - 3y = 4	Method 1:
Substitution method (since it is easy to isolate x.)	Solve the system of equations by the method of
$\begin{aligned} x - 3y &= 4\\ x &= 3y + 4 \end{aligned}$	your choice – this one lends itself to substitution.
2x - 5y + 12 = 0 2(3y + 4) - 5y + 12 = 0	Method 2:
6y + 8 - 5y + 12 = 0	Check by substituting each
y + 20 = 0 y = -20	equations to verify which point is a possible solution.
x = 4 + 3y	(_11 _14)
x = 4 + 3(-20) x = 4 - 60	(41, 14) 2x - 5y + 12 = 0
x = -56	2(-41) - 5(-14) + 12 = 0
	-82 + 70 + 12 = 0
(-56, -20)	0 = 0
Check:	x - 3y = 4
2x - 5y + 12 = 0	-41 - 3(-14) = 4 -11 + 52 = 1
2(-56) - 5(-20) + 12 = 0	
-112 + 100 + 12 = 0 True	
x - 3y = 4	(-44, -20)
(-56) - 3(-20) = 4	2x - 5y + 12 = 0
-56 + 60 = 4 True	2(-44) - 5(-20) + 12 = 0
	-88 + 100 + 12 = 0
Both are true, so $(-56, -20)$ is the correct solution.	24 7 0
	(-56, -12)
	2x - 5y + 12 = 0
	2(-56) - 5(-12) + 12 = 0
	-112 + 60 + 12 = 0
	-40 ≠ 0

Additional Resources:

Visions Volume 1, p. 39 (Mathematical Knowledge Summary) Khan Academy video: <u>http://www.khanacademy.org/math/algebra/systems-of-eq-and-ineq/fast-systems-of-equations/v/solving-systems-of-equations-by-elimination</u> Explore Learning Gizmos, <u>http://www.explorelearning.com/</u> look up: Systems of Linear Equations

Question: General Strategies: Stephane purchased 3 chocolate chip cookies and 4 peanut butter 1. Read the question. cookies for \$5.65. Marie purchased 5 chocolate chip cookies and 7 2. Highlight key words. peanut butter cookies for \$9.70. 3. Identify the math topic. What is the price of a peanut butter cookie? 4. Re-read the question. 5. Refer to your memory A) 70 cents aid, as needed. 6. Solve the problem B) 75 cents without looking at choices shown (A, B, C and D). C) 80 cents 7. Look at all the choices. D) 85 cents 8. Match your answer to the appropriate choice. Do not leave a blank! Make a choice! **My Strategies:**

Answer and Solution:	Suggested Strategies:	
x = cost of a chocolate chip cookie y = cost of a peanut butter cookie	Set up a system of equations and solve it.	
The answer is D.	 Define your variables Write your equations Choose a method (this one suggests elimination method but the other methods work as well.) Interpret your answer correctly by seeing which variable represents the cost of the peanut butter cookie. 	
Additional Resources:		
Visions Volume 1, pp. 39-40 (Mathematical Knowledge Summary) Khan Academy video: <u>http://www.khanacademy.org/math/algebra/systems-of-eq-and-ineq/fast-</u> <u>systems-of-equations/v/solving-systems-of-equations-by-elimination</u> Explore Learning Gizmos, <u>http://www.explorelearning.com/</u> look up: Systems of Linear Equations		

A kitchen cabinetmaker has two models of upper cupboards which a client can choose from to complete a kitchen installation.

Three different clients ordered different combinations of tall and short cabinets. The total cost including delivery is listed below for clients A and B.

Client	Number of Tall Cabinets	Number of Short Cabinets	Delivery Cost	Total Cost
А	7	4	\$120	\$1840
В	9	8	\$190	\$2630
С	11	2	\$170	?

Client C believes his total cost is lower than client B's.

Is he correct?

 \Box Yes

🗆 No

General Strategies:

- 1. Read the problem.
- 2. Highlight key words.
- Identify the math topics.
- 4. Re-read the problem.
- Define your steps (your game plan) – this is criteria 3.
- 6. Refer to your memory aid, as needed.
- 7. Solve.
- If you get stuck on a calculation, pick a number and keep going.
- 9. Ask yourself whether your answer makes sense.
- 10. Write your answer statement.

Show any or all your work! Do not leave a blank page!

My Strategies:

Answer and Solution:		Suggested Strategies:		
x = cost for long cabinety = cost for short cabinet		This is a "system of equations" question.		
Client A: 7x + 4y + 120 = 1840 Client B: 9x + 8y + 190 = 2630 Client C: 11x + 2y + 170 = ?	OR 7 <i>x</i> + 4 <i>y</i> = 1720 OR 9 <i>x</i> + 8 <i>y</i> = 2440	In order to find the cost for Client C, you need to know how much each type of cabinet costs.		
By elimination method: Step 1) -2(7x + 4y = 1720) 9x + 8y = 2440 -14x - 8y = -3440 9x + 8y = 2440 -5x = -1000 x = -1000 -5 x = 200	Step 2) 7x + 4y = 1720 7(200) + 4y = 1720 1400 + 4y = 1720 4y = 1720 - 1400 4y = 320 $y = \frac{320}{4} = 80$	 Use the information given for the other two clients to find those costs. Define your variables, Set up two equations in two unknowns, Solve the system, Use the solution to find the cost for Client C 		
x = 200 y = 80 Client C: $11x + 2y + 170 = ?$ 11(200) + 2(80) + 170 = 2200 + 160 + 170 = 2530 \$2530 Client C is correct. His total co is \$2530 compared to \$2630.	ost will be lower than client B's, since it	Note: if you don't show any work and just check one of the boxes, you will get zero.		
Additional Resources:				
Visions Volume 1, pp. 39-40 (Mathematical Knowledge Summary) Khan Academy video: <u>http://www.khanacademy.org/math/algebra/systems-of-eq-and-ineq/fast-systems-of-equations/v/solving-systems-of-equations-by-elimination</u>				

Explore Learning Gizmos, <u>http://www.explorelearning.com/</u> look up: Systems of Linear Equations

1.4 Half-Planes in the Cartesian Plane



Ans	wer and Solution:				Suggested Strategies:
Method 1:				Method 1:	
Plot Met	the point on each grap hod 2:	h and see which one is in t	he shad	ed area.	Begin by analyzing visually. Approximately where will point (100,200) be?
A B C D	$y \le -2x + 100$ $y > -2x + 100$ $y \le 100$ $x < 50$	$200 \le -2(100) + 100$ $200 \le -100$ $200 > -2(100) + 100$ $200 > -100$ $200 \le 100$ $100 < 50$	False True False False	50 and	Which graph will have that point in its shaded region? Method 2:
 A) Incorrect – the point has an <i>x</i>-coordinate to the right of 50 and that region is not shaded. B) Incorrect – the point has a <i>v</i>-coordinate that is above 100 and 			Write the rule for each graph and test the coordinates of the point		
 that region is not shaded. C) Correct – the point has an x-coordinate to the right of 50 and a y-coordinate above 100 and that region is shaded. 			in each one.		
D) Incorrect – the point has an x-coordinate to the right of 50 and that region is not shaded.					
The	answer is C.				
Additional Resources:					
Visio Khai	Visions Volume 1, Section 1.4, pp. 49-50 Khan Academy video: <u>http://www.khanacademy.org/math/algebra/linear-equations-and-</u> inequalitie/graphing-linear-inequalities/v/graphing-inequalities				



Answer and Solution:	Specific Strategies:			
-12.5x + 25y - 100 < 0 Test (0, 0) to see if the origin is in the solution set (and shaded).	Since all the lines are the same (same initial value, same slope) there is no			
-12.5(0) + 25(0) - 100 < 0	need to actually graph the given line.			
-100 < 0				
True	What is different among the 4 choices?			
Therefore the answer must be D.	 The shading is either above the line or 			
A) Incorrect – shading not below the line	 The line is either dashed or solid 			
B) Incorrect – solid line				
C) Incorrect – solid line	Since the inequality sign doesn't have the bar			
D) Correct – dashed line and shading below the line	eliminate choices B and C.			
	 Now to decide if the shading is above or below Test a point and see if the inequality is true. 			
The answer is D.				
Additional Resources:				
Visions Volume 1, Section 1.4, pp. 49-50				
Khan Academy video: - <u>http://www.khanacademy.org/math/algebra/linear-equations-and-</u>				
inequalitie/graphing-linear-inequalities/v/graphing-inequalities				



Answer and Solution:

Test for B only since A, C and D are eliminated.

Test (0, 0) in

0 > -3y - x + 75 $y > -\frac{1}{3}x + 25$ 0 > 0 + 25 0 > 25is false.

Put all the rules into function form and compare:

А	$y \le 75x + 25$	Not a dashed line
В	$y > -\frac{1}{3}x + 25$	Correct – dashed line and negative slope
С	$y \ge -\frac{1}{3}x + 25$	Not a dashed line
D	y > 75x + 25	Not a negative slope

Specific Strategies:

Method 1:

Process of elimination. Before doing any work, you can eliminate answers A and C because the graph has a dashed line and therefore the rule must have either a less than or greater than sign (<, >).

You can also determine that the slope is negative since the line is sloping down. This eliminates D since that slope is positive.

The answer is B.

Additional Resources:

Visions Volume 1, Section 1.4, pp. 49-50

Khan Academy video: <u>http://www.khanacademy.org/math/algebra/linear-equations-and-inequalitie/graphing-linear-inequalities/v/graphing-inequalities</u>

Question:	General Strategies:
Consider the inequality $4x - 2y < 8$ and point P (14, 24). Is point P a solution to the inequality?	 Read the question. Highlight key words. Identify the math topic. Re-read the question. Make a prediction about the answer- what will it look like? (an equation, a number, etc.). Refer to your memory aid, as needed. Solve. Ask yourself whether your answer makes sense. Write your answer. Do not leave a blank!
□ Yes, P is a solution to the inequality. □ No, P is not a solution to the inequality.	My Strategies:

Answer and Solution:	Suggested Strategies:		
P (14, 24) and $4x - 2y < 8$ 4(14) - 2(24) < 8 56 - 48 < 8 Since 8 is not less than 8, the statement is false and P is not in the solution set.	Check to see if that point, when plugged into the inequality, makes the statement true. If it's true, it is a solution. If it's false, it's not a solution.		
\Box Yes, P is a solution to the inequality.			
No, P is not a solution to the inequality.			
Additional Resources:			
Visions Volume 1, Section 1.4, pp. 49-50 Khan Academy video: <u>http://www.khanacademy.org/math/algebra/linear-equations-and-</u> inequalitie/graphing-linear-inequalities/v/graphing-inequalities			



Answer and Solution:			Suggested Strategies:	
Answei A B C D Answei 1. 2. 3. 4.	r and Solution: $ \begin{array}{c} -3x + y - 5 \ge 0 \\ -3x - 5 > -y \\ y - 5 \ge 0 \\ 0 \ge -x + 5 \end{array} $ rs: $ \begin{array}{c} c \\ B \\ -A \\ D \\ \end{array} $	$y \ge 3x + 5$ $y \ge 3x + 5$ $x \ge 5$	 Suggested Strategies: Put all of the inequalities into function form. Move <i>y</i> to the side where it will be positive (or the <i>x</i>, if there is no <i>y</i>.) Once they are all in function form, look for information which is particular to only 1 graph. Rule B is the only dashed line (>) so it must be graph 2. Rule A is the same as rule B except it is solid (≥) so it must be graph 3. Rule C has a constant slope so it must be graph 1. Rule D has an undefined slope (a vertical line) so it must be graph 4. 	
Additional Resources: Visions Volume 1, Section 1.4, pp. 49-50 Khan Academy video: <u>http://www.khanacademy.org/math/algebra/linear-equations-and-</u> ipogualitie/graphing_lipoar_ipogualities/w/graphing_ipogualities				

Juanita studies the layout of the IMAX theater by her house. Considering the angle of the seats, the width of the screen and the sound system, she comes up with a theory of where the best seats are.

She represents her theory as three inequalities on a Cartesian plane. The Cartesian plane represents the theater, and each of the intersections (lattice points) represents one seat.

Juanita's inequalities:

$$4x < -3y + 72$$
$$y < \frac{4}{3}x + 6$$
$$y \ge 10$$

The area where all three inequalities overlap contains the best seats.



How many of the seats can be considered the "best seats"?

General Strategies:

- 1. Read the problem.
- 2. Highlight key words.
- Identify the math topics.
- 4. Re-read the problem.
- Define your steps (your game plan) – this is criteria 3.
- 6. Refer to your memory aid, as needed.
- 7. Solve.
- If you get stuck on a calculation, pick a number and keep going.
- Ask yourself whether your answer makes sense.
- 10. Write your answer statement.

Show any or all your work! Do not leave a blank page!

My Strategies:



2.1 Diagrams and Statistics (Dispersion, Deviation, Stem and Leaf...)

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D)
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http://www.wikihow.com/Calculate-Mean-Deviation-About-Mean-(for-Ungrouped-Data)

Question: **General Strategies:** Which of the following statements is/are true concerning statistical 1. Read the question. measures? 2. Highlight key words. 3. Identify the math Ι. The mean, median, and range are measures of central topic. 4. Re-read the question. tendency. 5. Refer to your memory Π. Percentile rank is a measure of dispersion. aid, as needed. 6. Solve the problem III. without looking at The mean deviation and range are measures of dispersion. choices shown (A, B, IV. The mean deviation is a measure of position. C and D). 7. Look at all the choices. A) I only 8. Match your answer to the appropriate B) III only choice. Do not leave a blank! C) II and III only Make a choice! D) II and IV only **My Strategies:**

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Answ	ver and Solution:	Suggested Strategies:				
1.	The mean, median, and range are measures of central tendency. False – range is a measure of dispersion.	It is important to remember your vocabulary. Instead of				
11.	Percentile rank is a measure of dispersion. False – percentile is a measure of position.	blindly calculating mean, range etc. Try to think about why you are doing				
111.	The mean deviation and range are measures of dispersion. True.	them and what the result represents. This goes for any stats question.				
IV.	The mean deviation is a measure of position. False – mean deviation is a measure of dispersion.	 Recall: The measures of central tendency are mean, median, and mode. The measures of position are percentile rank Range and mean deviation are measures of dispersion. 				
The answer is B.						
Additional Resources:						
Vision Khan A proba	s Volume 2, pp. 81-82 Academy video: <u>https://www.khanacademy.org/math/cc-seventh</u> <u>bility-statistics/cc-7th-central-tendency/v/statistics-intromean</u>	n-grade-math/cc-7th- median-and-mode				

Consider the stem-leaf plot below showing the number of sit-ups students do in 60 seconds.

	Number of Sit-ups							
2	0 1 1 2 2 8 9							
3	2 2 3 4 5 6 6 8 9							
4	1 1 2 3 4 4 4 5 6 7 8							
5	0 1 1 2 5 6 6 7 8 8 8							
6	2466							

How many sit-ups did a student do if they are ranked in the 70th percentile?

- A) 35
- B) 36
- C) 51
- D) 52

General Strategies:

- 1. Read the question.
- 2. Highlight key words.
 3. Identify the math
- topic. 4. Re-read the guestion.
- 5. Refer to your memory aid, as needed.
- Solve the problem <u>without looking</u> at choices shown (A, B, C and D).
- 7. Look at all the choices.
- 8. Match your answer to the appropriate choice.

Do not leave a blank! Make a choice!



Ques	tion:	General Strategies:
At a la emplo below emplo 30, 32 146 en	arge company, a survey was conducted to see how fast byees can type. The company has 305 employees. The partial list shows the speed, in words per minute, achieved by the byees: 7, 32, 49, 50, 50, 50, 52, 53, 53, 89, 90, 93, 99 mployees 3 employees 156 employees	 Read the question. Highlight key words. Identify the math topic. Re-read the question. Refer to your memory aid, as needed. Solve the problem <u>without looking</u> at choices shown (A, B, C and D)
minut	e?	7. Look at all the
A)	47	 8. Match your answer to the appropriate
B)	48	choice. Do not leave a blank!
C)	49	Make a choice!
D)	50	My Strategies:

Answer and Solution:	Suggested Strategies:					
1 – Answer using the formula: $\frac{number \ of \ data \ value \ below \ or \ equal \ to \ x}{total \ number \ of \ data \ values}} \times 100$ $\frac{146 + 3}{305} \times 100 = \frac{149}{305} \times 100 \approx 48.85 \ round \ up \ to \ 49$ 2 – Answer using the formula: $\frac{number \ of \ data \ values \ below \ x + \frac{number \ of \ data \ values \ equal \ to \ x}{2} \times 100} \times 100$	The question is asking for percentile, so you need the formula which gives you the percentile of a data value. Be careful: Do not use the formula for finding a data value when the percentile is given					
$\frac{146 + \frac{3}{2}}{305} \times 100 = \frac{146 + 1.5}{305} \times 100 = \frac{147.5}{305} \times 100$ \$\approx 48.36 round up to 49\$	Remember to round to the next whole number (always UP!)					
A) 47 – if you don't take into account the 3 values at 50						
 B) 48 – if you round down or don't take into account the 3 values at 50 						
C) 49 – correct						
D) 50 – if you just take the value itself						
The answer is C.						
Additional Resources:						
Visions Volume 1, Section 2.1, pp. 76-88						

Consider the following set of data:

41 17 25 9 20 12 11 21 20

What is the mean deviation for the set of data?

General Strategies:

- 1. Read the question.
- 2. Highlight key words.
- 3. Identify the math topic.
- 4. Re-read the question.
- Make a prediction about the answerwhat will it look like? (an equation, a number, etc.).
- 6. Refer to your memory aid, as needed.
- 7. Solve.
- 8. Ask yourself whether your answer makes sense.
- 9. Write your answer. Do not leave a blank!

My Strategies:

The mean deviation for the set of data is _____.



The table below shows the finishing times for the 137 runners participating in a 5 km race:

18:48	26:36	29:22	31:34	35:08	38:04	48:58
20:01	26:37	29:29	31:55	35:09	38:45	48:58
21:19	26:43	29:29	32:13	35:09	38:59	49:50
21:55	26:48	29:30	32:26	35:35	39:21	49:51
23:36	26:54	29:30	32:28	35:39	39:22	50:01
23:36	27:20	29:31	32:28	35:45	39:38	53:40
24:15	27:38	29:49	32:36	36:11	40:52	56:19
24:29	27:50	29:56	32:50	36:11	41:07	56:20
24:34	27:50	30:02	32:56	36:12	41:35	57:06
24:34	27:56	30:03	32:57	36:24	41:35	59:12
24:35	28:32	30:08	33:07	36:25	44:44	59:14
25:01	28:42	30:28	33:09	36:25	44:45	59:18
25:04	28:45	30:31	33:14	36:27	46:01	1:00:55
25:08	28:45	30:31	33:30	37:21	46:15	1:01:05
25:08	28:59	30:34	33:39	37:21	46:22	1:03:39
25:44	29:02	30:39	33:46	37:25	46:24	1:03:42
25:58	29:04	31:07	33:46	37:43	47:05	1:03:46
26:19	29:13	31:25	33:46	37:54	47:19	
26:24	29:17	31:27	34:22	37:58	47:19	
26:31	29:17	31:29	34:43	38:03	48:11	

General Strategies:

- 1. Read the question.
- 2. Highlight key words.
- Identify the math topic.
- 4. Re-read the question.
- Make a prediction about the answerwhat will it look like? (an equation, a number, etc.).
- 6. Refer to your memory aid, as needed.
- 7. Solve.
- 8. Ask yourself whether your answer makes sense.
- 9. Write your answer.
- Do not leave a blank!

My Strategies:

- A) What is the percentile rank of the runners with a finishing time of 28 minutes 45 seconds?
- B) What is the finishing time of the runner who ranked in the 60th percentile?

The percentile rank of the runner finishing with 28:45 is _____.

The finishing time of the runner ranked in the 60th percentile is



The 20 best swimmers from across the country are trying out for the national swim team. To earn a spot on the team, a swimmer must meet both the following qualifications:

Qualification 1

The swimmer must rank better than the 60th percentile.

Qualification 2

The swimmer must have a "personal best time" (PBT) that is less than or equal to 20 seconds *minus* the mean deviation (MD) of the group.

 $PBT \le 20 - MD$

"Personal Best Times" (in seconds)

18.56	19.25	19.92	20.2
18.7	19.26	19.92	20.4
18.9	19.8	19.94	20.8
18.95	19.85	19.96	20.8
19.2	19.9	19.99	21.1

The mean of this distribution is 19.77 seconds.

How many of the 20 swimmers will earn a spot on the National team?

General Strategies:

- 1. Read the problem.
- 2. Highlight key words.
- Identify the math topics.
- 4. Re-read the problem.
- Define your steps (your game plan) – this is criteria 3.
- 6. Refer to your memory aid, as needed.
- 7. Solve.
- If you get stuck on a calculation, pick a number and keep going.
- 9. Ask yourself whether your answer makes sense.
- 10. Write your answer statement.

Show any or all your work! Do not leave a blank page!

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Answer and Solution:	Specific Strategies:
Qualification 1:	Remember that the lowest scores are the best
Swimmers that meet qualification 1:	scores. Therefore, the values in this distribution
$\frac{60}{100}(20) = 12$	are given in order of best to worst, not from worst
This means 12 swimmers are at or below the 60 th percentile.	to best (which is what we usually see). This makes
If 12 of the 20 swimmers are at or below the 60 th percentile, then 8 are above it.	finding the percentile a little bit tricky.
Qualification 2:	Make sure that your answer takes into account
Mean of the distribution: 19.77 (sum of all values \div 20)	the requirement to meet or exceed both of the
Mean deviation of the distribution: 0.557 (sum of all mean deviations \div 20)	evaluations that are used to select team members.
18.56 - 19.77 = 1.21 18.7 - 19.77 = 1.07	
: 21.1 – 19.77 = 1.33	
Sum of deviations = 11.14 11.14 ÷ 20 = 0.557	
Swimmers that meet qualification 2. PBT $\leq 20 - MD$ PBT $\leq 20 - 0.557$ PBT ≤ 19.443	
They are: 18.56, 18.7, 18.9, 18.95, 19.2, 19.25, 19.26	
Seven (7) swimmers will earn a spot on the National team.	
Additional Resources:	
Visions Volume 1, pp. 81-82	

2.2 Qualitative Interpretation of Correlation

Which of the following scatterplots shows the strongest linear correlation?



General Strategies:

- 1. Read the question.
- 2. Highlight key words.
- Identify the math topic.
- 4. Re-read the question.
- 5. Refer to your memory aid, as needed.
- Look carefully at each choice shown (A, then B, then C and then D).
- 7. Eliminate options you know to be incorrect.
- 8. Solve/check each possible choice.
- 9. Select the choice that makes the most sense.

Do not leave a blank! Make a choice!







At a recent school event, students were asked to sit facing the stage. The following table shows the distribution of students according to their ages and the distance from the stage.

DISTANCE (m) AGE (years)	[2,4[[4,6[[6,8[[8, 10[[10, 12[
[10,11[3	3	3	3	3
[11, 12[3	3	3	3	3
[12,13[3	3	3	3	3
[13,14[3	3	3	3	3
[14, 15[3 -	3	3	3	3

Which of the following best describes the linear correlation between the age of the students and the distance from each student to the stage?

- A) The correlation is positive.
- B) The correlation is negative.
- C) The correlation is perfect.
- D) The correlation is zero.

General Strategies:

- 1. Read the question.
- 2. Highlight key words.
- Identify the math topic.
- 4. Re-read the question.
- 5. Refer to your memory aid, as needed.
- Look carefully at each choice shown (A, then B, then C and then D).
- 7. Eliminate options you know to be incorrect.
- 8. Solve/check each possible choice.
- Select the choice that makes the most sense.

Do not leave a blank! Make a choice!

Answer and Solution:								Specific Strategies:
	DISTANCE (m) AGE (years)	[2,4[[4,6[[6,8[[8, 10[[10, 12[The closer the data is to the
	[10,11[3	3	3	3	3		diagonal, the
	[11, 12[3	3	3	3	3	1	correlation.
	[12,13[3	3	3	3	3		
	[13,14[3	3	3	3	3]	
	[14,15[3	3	3	3	3		
In a table, the closer the data is to the diagonal, the stronger the correlation. All values are 3 so data is not clustered on the diagonal. In this case, the data is evenly spread out, thus indicating no correlation.								A correlation may be zero, weak, moderate, strong or perfect!
A)	The correlation is positive – false: data is not clustered around a diagonal from top left to bottom right.							
B)	The correlation is negative – false: data is not clustered around a diagonal from bottom left to top right.							
C)	C) The correlation is perfect – false: given an age, there is no way to predict the distance from the stage.							
D) The correlation is zero – true: given an age, there is no way to predict the distance from the stage.								
The answer is D.								
Additi	Additional Resources:							
Visions	Volume 1, S	ection 2.	2, pp. 93	-94				

Consider the following table showing a two-variable distribution. Indicate the strength and direction of correlation.

y x	[0,1[[1,2[[2,3[[3,4[[4,5[
1	2	0	0	0	0
2	0	2	0	0	0
3	0	3	2	2	0
4	0	0	0	5	2
5	0	0	0	1	1

General Strategies:

- 1. Read the question.
- 2. Highlight key words.
- 3. Identify the math topic.
- 4. Re-read the question.
- Make a prediction about the answerwhat will it look like? (an equation, a number, etc.).
- 6. Refer to your memory aid, as needed.
- 7. Solve.
- 8. Ask yourself whether your answer makes sense.
- 9. Write your answer.
- Do not leave a blank!

My	Strate	gies:
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<u>Strength</u>	<u>Direction</u>
🗆 Weak	□ Positive
□ Strong	□ Negative

Answer and Solution:				Suggested Strategies:		
Answer an	nd Solution	n: [1,2[0 2 3 0 0 0	[2,3[0 0 2 0 0	[3,4[0 0 2 5 1	[4,5] 0 0 2 1	 Suggested Strategies: In a table, the closer the data is to the diagonal, the stronger the correlation. If the diagonal slopes downward, then the correlation is positive – because as <i>x</i> increases, so does <i>y</i>.
The answer Strength □ Weak ☑ Strong Additiona Visions Volu	is: I Resource	<u>Dire</u> ☑ F □ N 25: on 2.2, pp. 9	<u>ction</u> Positive Negative 93-94			

Consider the following scatterplot.

- A) Is the correlation weak or strong?
- B) Is the direction positive or negative?



General Strategies:

- 1. Read the question.
- 2. Highlight key words.
- 3. Identify the math topic.
- 4. Re-read the question.
- Make a prediction about the answerwhat will it look like? (an equation, a number, etc.).
- 6. Refer to your memory aid, as needed.
- 7. Solve.
- 8. Ask yourself whether your answer makes sense.
- 9. Write your answer. Do not leave a blank!

		My Strategies:
<u>Strength</u>	Direction	
🗆 Weak	□ Positive	
□ Strong	□ Negative	
		1

Answer and Solution:		Specific Strategies:
	 The points appear to form a descending line (negative direction) The points are very scattered far apart (weak correlation) 	Look at how far or close the points are relative to each other
×,		 The closer the points are to forming a straight line, the stronger the correlation is A positive slope means a positive correlation A negative slope means a negative correlation
The answer is:		
<u>Strength</u>	Direction	
🗹 Weak	□ Positive	
□ Strong	☑ Negative	
Additional Resources:		1
Visions Volume 1, Section 2.2 Explore Learning Gizmos, <u>http</u> Correlation Trends in Scatter Plots Scatter Plots-Activity	e, pp. 93-95 <u>p://www.explorelearning.com/</u> look up: s	

2.3 Quantitative Interpretation of Correlation

Consider the following linear correlation coefficients.

-0.81,0.39,-0.27,0.74

Which of the following lists the correlation coefficients from weakest to strongest?

- A) -0.81, 0.74, 0.39, -0.27
- B) -0.27, 0.39, 0.74, -0.81
- C) -0.81 , -0.27 , 0.39 , 0.74
- D) 0.74, 0.39, -0.27, -0.81

General Strategies:

- 1. Read the question.
- 2. Highlight key words.
- 3. Identify the math topic.
- 4. Re-read the question.
- 5. Refer to your memory aid, as needed.
- Look carefully at each choice shown (A, then B, then C and then D).
- 7. Eliminate options you know to be incorrect.
- 8. Solve/check each possible choice.
- 9. Select the choice that makes the most sense.

Do not leave a blank! Make a choice!



Question:	General Strategies:
Which of the following correlation coefficient shows the weakest correlation?	 Read the question. Highlight key words. Identify the math
A) –0.75	topic.
B) –0.45	 Re-read the question. Refer to your memory
C) 0.16	aid, as needed. 6. Look carefully at each
D) 0.83	 choice shown (A, then B, then C and then D). 7. Eliminate options you know to be incorrect. 8. Solve/check each possible choice. 9. Select the choice that makes the most sense. Do not leave a blank! Make a choice! My Strategies:



Question:	General Strategies:
Question: Which of the following correlation coefficients shows a perfect correlation? A) -1.00 B) -0.10 C) 0.00 D) 0.99	 General Strategies: Read the question. Highlight key words. Identify the math topic. Re-read the question. Refer to your memory aid, as needed. Look carefully at each choice shown (A, then B, then C and then D). Eliminate options you know to be incorrect. Solve/check each possible choice. Select the choice that makes the most sense. Do not leave a blank! Make a choice!
	makes the most sense. Do not leave a blank! Make a choice!
	My Strategies:



Consider the following scatterplot.



What is the linear correlation coefficient?

General Strategies:

- 1. Read the question.
- 2. Highlight key words.
- Identify the math topic.
- 4. Re-read the question.
- Make a prediction about the answerwhat will it look like? (an equation, a number, etc.).
- 6. Refer to your memory aid, as needed.
- 7. Solve.
- 8. Ask yourself whether your answer makes sense.
- 9. Write your answer. Do not leave a blank!

My Strategies:

The linear correlation coefficient is ______.



Consider the following scatterplot.



Estimate the linear correlation coefficient.

General Strategies:

- 1. Read the question.
- 2. Highlight key words.
- Identify the math topic.
- 4. Re-read the question.
- Make a prediction about the answerwhat will it look like? (an equation, a number, etc.).
- 6. Refer to your memory aid, as needed.
- 7. Solve.
- 8. Ask yourself whether your answer makes sense.
- 9. Write your answer. Do not leave a blank!

My Strategies:

The linear correlation coefficient is ______.


The Granby Zoo feeds its elephants daily. The chart below shows the weight of several elephants and the weight of the food they are given every day.

Weight of elephant (kg)	Weight of food (kg)
1250	58
1300	63
1320	66
1382	69
1400	67
1460	63
1480	70
1492	76

How much food would an elephant weighing 1600 kg be given? Round your answer to the nearest tenth of a kilogram. **General Strategies:**

- 1. Read the problem.
- 2. Highlight key words.
- Identify the math topics.
- 4. Re-read the problem.
- Define your steps (your game plan) – this is criteria 3.
- 6. Refer to your memory aid, as needed.
- 7. Solve.
- If you get stuck on a calculation, pick a number and keep going.
- 9. Ask yourself whether your answer makes sense.
- 10. Write your answer statement.

Show any or all your work! Do not leave a blank page!

My Strategies:

A 1600kg elephant would be given _____ kg of food.



2.4 Interpretation of Linear Correlation

Which of the following distributions suggests a linear correlation of the data?



General Strategies:

- 1. Read the question.
- 2. Highlight key words.
- Identify the math topic.
- 4. Re-read the question.
- 5. Refer to your memory aid, as needed.
- Look carefully at each choice shown (A, then B, then C and then D).
- 7. Eliminate options you know to be incorrect.
- 8. Solve/check each possible choice.
- 9. Select the choice that makes the most sense.

Do not leave a blank! Make a choice!

Answer and Solution:		Suggested Strategies:
A)	This data is clustered along a line	The graph that shows data points that closely form a straight line yields the best interpretations
B)	This data is clustered along a curve (not linear)	for linear correlation
C)	∴ This data has a large gap and therefore a straight linear correlation can't be assumed	
D)	This data is clustered in one area rather than along a line	
The ans	swer is A.	
Additi	onal Resources:	
Visions Volume 1, Section 2.4, pp. 123-124 Khan Academy Video: <u>http://www.khanacademy.org/math/probability/regression/regression-</u> <u>correlation/v/fitting-a-line-to-data</u> see: Fitting a Line to Data, Estimating the Line of Best Fit Explore Learning Gizmos, <u>http://www.explorelearning.com/</u> look up: Scatter Plots Activity A, Solving Using Trend Lines		



Answer and Solution:	Suggested Strategies:
B) – the data points in this graph are closest to forming a line.	The graph showing the strongest correlation, whether positive or negative, would demonstrate the strongest statistical link between two variables. A strong statistical link leads to better prediction.
The answer is B.	

Additional Resources:

Visions Volume 1, Section 2.4, pp. 123-124

Khan Academy Video: <u>http://www.khanacademy.org/math/probability/regression/regression-correlation/v/fitting-a-line-to-data</u> see: Fitting a Line to Data, Estimating the Line of Best Fit Explore Learning Gizmos, <u>http://www.explorelearning.com/</u> look up: Scatter Plots Activity A, Solving Using Trend Lines

http://www.purplemath.com/modules/scattreg2.htm

The linear correlation coefficient between two variables is -0.93.

Which of the following best describes the correlation?

- A) The correlation between the two variables is strong and positive.
- B) The correlation between the two variables is strong and negative.
- C) The correlation between the two variables is weak and positive.
- D) The correlation between the two variables is weak and negative.

General Strategies:

- 1. Read the question.
- 2. Highlight key words.
- Identify the math topic.
- 4. Re-read the question.
- 5. Refer to your memory aid, as needed.
- Look carefully at each choice shown (A, then B, then C and then D).
- 7. Eliminate options you know to be incorrect.
- 8. Solve/check each possible choice.
- 9. Select the choice that makes the most sense.

Do not leave a blank! Make a choice!

Answer and Solution:		Suggested Strategies:
A)	False: The correlation between the two variables is strong and not positive.	The options are all wordy but you will see that they are almost exactly the
B)	The correlation between the two variables is strong and negative.	same; look for the differences – you might
C)	False: The correlation between the two variables is not weak and positive.	The correlation coefficient
D)	False: The correlation between the two variables is not weak and negative.	this results in a correlation described as negative and strong.
The ar	ıswer is B.	
Additional Resources:		

Visions Volume 1, Section 2.4, pp. 123-124

Khan Academy Video: <u>http://www.khanacademy.org/math/probability/regression/regression-correlation/v/fitting-a-line-to-data</u> see: Fitting a Line to Data, Estimating the Line of Best Fit Explore Learning Gizmos, <u>http://www.explorelearning.com/</u> look up: Scatter Plots Activity A, Solving Using Trend Lines

http://www.dummies.com/how-to/content/how-to-interpret-a-correlation-coefficient-r.html

Question: Gen	eral Strategies:
The linear correlation between two variables is positive and weak.1.Which of the following could represent the correlation coefficient?2.	Read the question. Highlight key words. Identify the math
A) 0.32	topic.
B) 0.87 5.	Refer to your memory
C) -0.26 6.	Look carefully at each
D) -0.91 7. 8. 9. Do n Mak My 1	choice shown (A, then B, then C and then D). Eliminate options you know to be incorrect. Solve/check each possible choice. Select the choice that makes the most sense. ot leave a blank! e a choice! Strategies:

Answer and Solution:		Suggested Strategies:
A)	0.32 – close to 0 and positive	A weak and positive
В)	0.87 – positive but not close to 0	represented by a correlation coefficient
C)	–0.26 – closest to 0 but negative	value that is positive and much closer to 0 than to
D)	-0.91 - negative and not close to 0	1.
The a	nswer is A.	
Additional Resources:		
Visions Volume 1, Section 2.4, pp. 123-124 Khan Academy Video: <u>http://www.khanacademy.org/math/probability/regression/regression-correlation/v/fitting-a-line-to-data</u> see: Fitting a Line to Data, Estimating the Line of Best Fit Explore Learning Gizmos, <u>http://www.explorelearning.com/</u> look up: Scatter Plots Activity A, Solving Using Trend Lines		



Answer and Solution: **Specific Strategies:** A) Strong and positive This scatterplot shows data points that trend B) Strong and negative downward suggesting a negative correlation. C) Weak and positive This scatterplot also D) Weak and negative shows data points that are spread apart rather than close together (along a line) suggesting a weak correlation. The answer is D. **Additional Resources:** Visions Volume 1, Section 2.4, pp. 123-124 Khan Academy Video: http://www.khanacademy.org/math/probability/regression/regressioncorrelation/v/fitting-a-line-to-data see: Fitting a Line to Data, Estimating the Line of Best Fit Explore Learning Gizmos, http://www.explorelearning.com/ look up: Scatter Plots Activity A,

Solving Using Trend Lines



Answer and Solution: Suggested Strategies: A) 0.29 – positive by not high enough so suggest a strong This scatterplot shows correlation data points that trend upward therefore you are B) looking for a positive 0.83 – positive and high enough to suggest a strong correlation coefficient. correlation This scatterplot also C) -0.45 – a negative correlation, and not very strong shows data points that -0.79 – a negative correlation, even though it is fairly strong. are close together (along D) a line) rather than spread out so you are looking for a correlation coefficient that suggests a strong correlation. The answer is B. **Additional Resources:** Visions Volume 1, Section 2.4, pp. 123-124 Khan Academy Video: http://www.khanacademy.org/math/probability/regression/regressioncorrelation/v/fitting-a-line-to-data see: Fitting a Line to Data, Estimating the Line of Best Fit Explore Learning Gizmos, http://www.explorelearning.com/ look up: Scatter Plots Activity A, Solving Using Trend Lines

A class of secondary 4 students measured their foot lengths and their heights. They then found a linear regression equation for their data. This equation would be used to predict the foot length of Marco, who was absent the day the data was collected.

Data Collected			
Foot length	Height (cm)	Foot length	Height (cm)
(cm)		(cm)	
22	154	25.5	170
22	151	25.5	173
23	155	26	167
23.5	165	27	174
24	160	27.5	175
24	158	28	176
24.5	165	28	183
25	161	28.5	185
25	163	29	190
25.5	164	29.5	186

Marco is 181 cm tall.

What is the predicted length of Marco's foot?

General Strategies:

- 1. Read the problem.
- 2. Highlight key words.
- Identify the math topics.
- 4. Re-read the problem.
- Define your steps (your game plan) – this is criteria 3.
- 6. Refer to your memory aid, as needed.
- 7. Solve.
- If you get stuck on a calculation, pick a number and keep going.
- 9. Ask yourself whether your answer makes sense.
- 10. Write your answer statement.

Show any or all your work! Do not leave a blank page!

My Strategies:

Marco's predicted foot length is .

Answer and Solution:	Suggested Strategies:	
With the Mayer line method: x represents the foot length in centimetres y represents the height in centimetres Since the foot lengths are already in ascending order this step has been done for us. x ₁ = $22+22+23+23+24+24+24+52+25+25+5 = 23.85$ 10 x ₂ = $25.5+25.5+26+27+27.5+28+28+28+28+29+29.5$ 10 = 27.45 y ₁ = $\frac{154+151+155+165+160+158+165+161+163+164}{10}$ = $\frac{1596}{10}$ y ₂ = $\frac{170+173+167+174+175+176+183+185+190+186}{10}$ = $\frac{177.9}{10}$ a = $\frac{177.9-159.6}{17.9-159.6} = \frac{183}{3} = 5.08$ 27.45 - 23.85 3.6 y = $5.08x + b$ using either point (23.85, 159.6) 159.6 = $5.08(23.85) + b$ or (27.45, 177.9) 159.6 = $121.16 + b$ b = 38.44 y = $5.08x + 38.44$ Marco: $181 = 5.08x + 38.44$	 What you are looking for is a linear equation relating height and foot length. Once you've found one, you will use it to find foot length, knowing height. There are a number of methods possible. Complete a scatter plot, drawing in the line of best fit and finding the equation of that line Use the median- median method Use the Mayer line method Enter the data into a graphing calculator to get the regression line 	
Additional Resources:		
Visions Volume 1, Section 2.4, pp. 123-124 Explore Learning Gizmos, <u>http://www.explorelearning.com/</u> look up: Scatter Plots Activity A, Solving using trend lines Khan Academy video: <u>http://www.khanacademy.org/math/probability/regression/regression- correlation/v/fitting-a-line-to-data</u> see fitting a line to data, estimating the line of best fit		

3.1 Congruent Triangles

Question: General Strategies: Which of the following pairs of triangles is not necessarily congruent? 1. Read the question. 2. Highlight key words. A) 3. Identify the math topic. 4. Re-read the question. 5. Refer to your memory aid, as needed. 6. Look carefully at each B) choice shown (A, then B, then C and then D). 7. Eliminate options you know to be incorrect. 8. Solve/check each possible choice. C) 9. Select the choice that makes the most sense. Do not leave a blank! Make a choice! D) **My Strategies:**

Answer and Solution:		Suggested Strategies:
A)	This is the correct answer. These triangles are <i>not necessarily</i> congruent since they only have two congruent sides and no congruent angles indicated.	Check all possible answers, and beside each one write the proof that
B)	These are congruent by ASA.	should be left with only
C)	These are congruent by SSS (because the unmarked angles are necessarily congruent.)	(meaning those triangles are <i>not</i> congruent).
D)	These are congruent by ASA.	
The a	nswer is A.	
Additional Resources:		
Visions Volume 1, Section 3.1, pp. 149-151, pp. 160-161 Explore Learning Gizmos, <u>http://www.explorelearning.com/</u> look up: Proving triangles congruent Khan Academy video:		
Additional Resources: Visions Volume 1, Section 3.1, pp. 149-151, pp. 160-161 Explore Learning Gizmos, <u>http://www.explorelearning.com/</u> look up: Proving triangles congruent Khan Academy video: <u>http://www.khanacademy.org/search?page_search_query=congruent+triangles_</u> Congruent		

triangles (all conditions: SSS, ASA and SAS)

Consider the following diagram.



What theorem can be used to show that ΔABD is necessarily congruent to $\Delta ACD?$

- A) SSS
- B) SAS
- C) ASA
- D) None, they are not necessarily congruent.

General Strategies:

- 1. Read the question.
- 2. Highlight key words.
- Identify the math topic.
- 4. Re-read the question.
- 5. Refer to your memory aid, as needed.
- Solve the problem without looking at choices shown (A, B, C and D).
- 7. Look at all the choices.
- Match your answer to the appropriate choice.

Do not leave a blank! Make a choice!

Answer and Solution:	Suggested Strategies:	
The diagram identifies pairs of congruent angles and even though the congruent sides are not identified, the triangles share a side, which makes it congruent. Since the shared side is between pairs of congruent angles, the proof ASA is valid to prove congruency.	When proving congruency (≅), first consider the three possible proofs (SSS, SAS, ASA). Starting with this will likely help you to eliminate one or two of the proofs as not having enough information pretty quickly. Although this proof is perhaps not obvious since the congruent sides aren't identified, don't overlook the fact that the triangles share a side (AD).	
The answer is C.		
Additional Resources:		
Visions Volume 1, Section 3.1, pp. 149-151, pp. 160-161 Explore Learning Gizmos, <u>http://www.explorelearning.com/</u> look up: Proving triangles congruent Khan Academy video:		

http://www.khanacademy.org/search?page_search_query=congruent+triangles_Congruent triangles (all conditions: SSS, ASA and SAS)

Which of the following pairs of triangles is necessarily congruent?



General Strategies:

- 1. Read the question.
- 2. Highlight key words.
- Identify the math topic.
- 4. Re-read the question.
- 5. Refer to your memory aid, as needed.
- Look carefully at each choice shown (A, then B, then C and then D).
- 7. Eliminate options you know to be incorrect.
- 8. Solve/check each possible choice.
- 9. Select the choice that makes the most sense.

Do not leave a blank! Make a choice!

Answer and Solution: Suggested Strategies: Although the top angle is not identified as being congruent in the two Don't be discouraged if triangles in answer b, they must be since the other two pairs of the correct answer corresponding angles are the same. Since the unidentified angles are doesn't jump out at you now known to be congruent, two theories can be used to prove right away! Even though congruency – ASA and SAS. this is a multiple choice question, and you might A) There is not enough information, having two angles the same expect to see the answer makes the triangle similar but not necessarily congruent right away, there is often work or extra thinking B) This may look like ASA but the congruent sides are not needed to uncover the between the congruent angles so you can't conclude the correct answer. Don't give triangles are congruent by that theory. up until you've tried all possibilities, in this case it This is the correct answer. involved a little extra C) thought. D) This pair doesn't have corresponding sides that are congruent so you can't conclude they are congruent by ASA. The answer is C. Additional Resources:

Visions Volume 1, Section 3.1, pp. 149-151, pp. 160-161 Explore Learning Gizmos, <u>http://www.explorelearning.com/</u> look up: Proving triangles congruent Khan Academy video: <u>http://www.khanacademy.org/search?page_search_query=congruent+triangles_</u>Congruent triangles (all conditions: SSS, ASA and SAS)



Answer and Solution:	Suggested Strategies:
If P is the midpoint of MN, then MP and NP are congruent sides of the triangles. It should be said that <lpm <opn="" and="" are="" vertically<br="">opposite and therefore congruent and that <pml <pno="" and="" are<br="">alternate interior angles of a transversal through parallel lines, which means those angles are congruent as well. With that information, we can say the triangles are necessarily congruent using the ASA proof.</pml></lpm>	Make sure you fill in all the information that you know on your diagrams. This is important on all questions of a test, but especially on ones where there is obviously information that has been left out. Don't forget all of the angle relationships when filling in information – and seeing a transversal through parallel lines should remind you of those angle relationships.
$\overline{MP} \cong \overline{PN}$	
$<$ LPM \cong $<$ OPN	
$<$ PML \cong $<$ PNO	
$\Delta LMP \cong \Delta ONP$ by <u>ASA</u>	
Additional Resources:	
Visions Volume 1 Section 3.1 np. 149-151 np. 160-161	

Visions Volume 1, Section 3.1, pp. 149-151, pp. 160-161 Explore Learning Gizmos, <u>http://www.explorelearning.com/</u> look up: Proving triangles congruent Khan Academy video: <u>http://www.khanacademy.org/search?page_search_query=congruent+triangles_</u>Congruent triangles (all conditions: SSS, ASA and SAS)

Question: General Strategies: Consider the following diagram. 1. Read the question. 2. Highlight key words. 3. Identify the math topic. 4. Re-read the question. 5. Make a prediction С about the answerwhat will it look like? (an equation, a number, etc.). 6. Refer to your memory Prove that $\triangle ABC$ is necessarily congruent to $\triangle EDC$. aid, as needed. 7. Solve. _____ ≅ _____ 8. Ask yourself whether your answer makes _____≅ _____ sense. 9. Write your answer. _____≅ _____ Do not leave a blank! **My Strategies:** $\Delta ABC \cong \Delta EDC$ by _____

Answer and Solution:	Suggested Strategies:	
This diagram shows only two pairs of sides are congruent so you can eliminate ASA. That leaves SSS and SAS. But you know that vertically opposite angles are necessarily congruent even if they aren't identified.	When proving congruency consider the three possible proofs (SSS, SAS, ASA). Starting with this will likely help you to eliminate one or two of the proofs as not having enough information pretty quickly.	
	In other cases, don't forget to go through the possible angle relationships for intersecting and transverse lines across parallel lines.	
$\overline{AC} \cong \overline{EC}$		
$\angle ACB \cong \angle ECD$		
$\overline{BC} \cong \overline{DC}$		
$\Delta ABC \cong \Delta EDC$ by SAS		
Additional Resources:		
Visions Volume 1, Section 3.1, pp. 149-151, pp. 160-161 Explore Learning Gizmos, <u>http://www.explorelearning.com/</u> look up: Proving triangles congruent Khan Academy video: <u>http://www.khanacademy.org/search?page_search_query=congruent+triangles</u>		

Question:	General Strategies:
You've been hired to paint a team logo on a field for a sporting event. The logo consists of two congruent triangles. Model of the logo consists of two congruent triangles. Model of the logo consists of two congruent triangles that Here is the information you have: Point P is the midpoint of MN M is located at (-60, 48) N is located at (-60, 48) N is located at (28, 4) ZLMP measures 95°	 Read the problem. Highlight key words. Identify the math topics. Re-read the problem. Define your steps (your game plan) – this is criteria 3. Refer to your memory aid, as needed. Solve. If you get stuck on a calculation, pick a number and keep going. Ask yourself whether your answer makes sense. Write your answer statement. Show any or all your work! Do not leave a blank page! My Strategies:
make up the logo.	

Answer and Solution:

Step 1) Calculate the coordinates of P using the midpoint formula. They are (-16, 26).

 $\begin{array}{l} (x_m, y_m): \left(\underbrace{ (-60+28)}_2, \underbrace{ (48+4)}_2 \right) \\ (x_m, y_m): \quad \left(\underbrace{ (-32)}_2, \underbrace{ (52)}_2 \right) \\ (x_m, y_m): \quad (-16, 26) \end{array}$

OR Calculate the distance between the two points and divide that distance by 2.

Step 2) Calculate the distance from M to P. It is 49.1935 metres.

 $d = \sqrt{(-16 - -60)^2 + (26 - 48)^2}$ $d = \sqrt{(44)^2 + (-22)^2}$ $d = \sqrt{1936 + 484}$ $d = \sqrt{2420}$ d = 49.1935 metres

Step 3) The missing angle (<MLP) is 70°. Using the Sine Law, calculate the missing measurements for Δ LMP. We know side MP is 49.1935 metres, we can calculate side LM. It is 52.15 metres. We can then calculate side LP. It is 13.55 metres.

$$\frac{49.1935}{sin70} = \frac{x}{sin15} = \frac{y}{sin95}$$

$$x = \frac{49.1935(sin15)}{sin70}$$

$$x = 13.55 metres (side LP)$$

$$y = \frac{49.1935(sin95)}{sin70}$$

$$y = 52.15 metres (side LM)$$

Step 4) Calculate the area of Δ LMP using either the Trig Formula or Hero's Formula. It is 332 m² (rounded to the nearest square meter).

Example of Trig Formula: Area = $\frac{(13.55)(52.15)(sin70)}{2}$ = 332 metres²

OR Hero's Formula:

Half the perimeter: $\frac{49.19+13.55+52.15}{2} = 57.45$ $Area = \sqrt{57.45(57.45 - 49.19)(57.45 - 13.55)(57.45 - 52.15)}$ $Area = \sqrt{57.45(8.26)(43.9)(5.3)}$ $Area = \sqrt{110410.52379}$ $Area = 332 \text{ metres}^2$

Step 5) Multiply the area of ΔLMP by 2, then multiply that by \$5. The total cost of painting is \$3320. (332m² x 2 x \$5/m² = \$3320)

You will charge <u>\$3320</u> for painting the two triangles that make up the logo.

Additional Resources:

Visions Volume 1, Section 3.1, pp. 149-151, pp. 160-161 Khan Academy video: <u>http://www.khanacademy.org/search?page_search_query=congruent+triangles</u> Congruent triangles (all conditions: SSS, ASA and SAS Explore Learning Gizmos, <u>http://www.explorelearning.com/</u>look up: Proving triangles congruent <u>http://mathbits.com/MathBits/TISection/Trig/AreaTrigTri.htm</u>

Suggested Strategies:

You need to find the area of the triangles and multiply that by \$5.

What do you need to find the area of a triangle?

- The length of a base and altitude or
- The length of two sides and the angle between them (Trig area formula) or
- The length of all three sides (Hero's Formula)

Choose the method you think will work for you and find the measures you need.

You only need to do this once since the triangles are congruent.

3.2 Similar Triangles


Answer and Solution:	Specific Strategies:		
16cm			
A 8cm E 5cm B B C D	Some distractors might stand out: choices A) and B) are both fairly small, whereas C) and D) are both fairly large. An educated guess would eliminate A) and B), but we should remember that the drawings are never to scale.		
$\triangle ABC \sim \triangle DEC$ because of the AA theorem – angle C is the same in both triangles, and because they are vertically opposite, $\angle E \cong \angle B \text{ (and } \angle D \cong \angle A \text{)}$ because they are alternate interior angles.	 Label the figure with the given 		
In order to determine the total length of \overline{BE} , we need the length of \overline{CE} , so label the measure of \overline{CE} as "x".	measurements - Recognize that the		
Since the triangles are similar, their sides must be proportional. Set up a proportion using corresponding sides:	triangles are similar because of AA		
$\frac{m\overline{CE}}{m\overline{BC}} = \frac{m\overline{ED}}{m\overline{AB}} \longrightarrow \frac{x}{12} = \frac{5}{16}$	Alternate strategy:		
Cross multiply to determine the value of x $x = 12 \times 5 \div 16 = 3.75 \text{ cm}$	<i>k</i> by dividing the lengths of corresponding sides: <i>k</i> =		
To determine the length of side BE, add $m\overline{BC} + m\overline{CE}$ 12 + 3.75 = 15.75cm	3.2 Divide side BC by 3.2 to		
A) 2.5 cm is the measure of segment CD.	get the length of side CE = 3.75cm		
 B) 3.75 cm is the measure of segment EC. The measure of segment BC must be added to this. 	 After completing the calculations. re-read 		
C) The result of adding the measures of segments CD and BC instead of EC and BC.	the question and re- read the choices		
D) 15.75 cm is correct.			
The answer is D.			
Additional Resources: Visions Volume 1, Section 3.2, p. 171 (Minimum Conditions for Similar Triangles) Khan Academy video:http://www.khanacademy.org/math/geometry/similarity/triangle			

similarlity/v/similarity-example-problems Similarity example problems

QUESTION 57



Answer and Solution:		Sp	pecific Strategies:
$m \angle y = 180^{\circ} - 105^{\circ} - 27^{\circ} = 48^{\circ}$ since the angles in every triangle add up to 180°		-	Keyword: Similar Recall theorems on
A) B)	Incorrect: This triangle only has one angle in common with triangle XYZ. Two side measures are given, but it is only possible to compare with one side of XYZ and we need at least two sides to prove SSS or SAS. (If you used the Sine Law to find the missing side of the original triangle, you will also see that the sides are not proportional.) Incorrect: This triangle gives us three side measurements, but like option A, we would need to be able to compare at least	- - 1 -	similar triangles Determine the measure of the third angle in triangle XYZ Triangles are similar if they satisfy one of three theorems – AA, SSS or SAS
C)	two sides to prove SSS or SAS. Correct: This triangle is similar to XYZ. It has two angles in common because the third angle was calculated above to be 48°. So by AA, the triangles are similar.		
D)	Incorrect: This triangle is not necessarily similar to XYZ because the information the triangle is not unique – you can make many triangles with those three features fixed.		
The ar	nswer is C.		
Additional Resources:			
Visions Volume 1, Section 3.2, p. 171 (Minimum Conditions for Similar Triangles) Khan Academy video: <u>http://www.khanacademy.org/math/geometry/similarity/triangle</u> <u>similarlity/v/similarity-example-problems</u> Similarity example problems			

Question:	General Strategies:
In the diagram below, \overline{BD} and \overline{AE} intersect at C Other measurements are given: $m\overline{AC} = 30m$ $m\overline{BC} = 25m$ $m\overline{CD} = 15m$ $m\overline{CE} = 18m$ Which of the following statements could be used to prove that triangle ABC is similar to triangle EDC?	 Read the question Highlight key words Identify the math topic Re-read the question Refer to your memory aid, as needed Look carefully at each choice shown (A, then B, then C and then D) Eliminate options you know to be incorrect Solve/check each possible choice Select the choice that makes the most sense Do not leave a blank! Make a choice!
 A) Two triangles with corresponding angles congruent are similar. (AA) 	My Strategies:
 B) Two triangles whose measures of corresponding sides are proportional, are similar. (SSS) 	
C) If two angles of one triangle are congruent to two angles of another triangle, and the contained sides are proportional, then the triangles are similar. (ASA)	
D) Two triangles having a congruent angle contained between the corresponding sides of proportional lengths are similar. (SAS)	



С



In the figure below, triangles ABC and ADE are similar.

What is the length of segment EC?

General Strategies:

- 1. Read the question.
- 2. Highlight key words.
- 3. Identify the math topic.
- 4. Re-read the question.
- Make a prediction about the answerwhat will it look like? (an equation, a number, etc.).
- 6. Refer to your memory aid, as needed.
- 7. Solve.
- 8. Ask yourself whether your answer makes sense.
- 9. Write your answer.
- Do not leave a blank!

My	Strate	egies:
		0

The length of segment EC is ______ m.



<u>similarlity/v/similarity-example-problems</u> Similarity example problems





The following measures are given for the figure below:

$m\overline{AD} = 12cm$ $m\overline{DB} = 4cm$ $m\overline{AE} = 8cm$ $m\overline{EC} = 16cm$
c
Is triangle $\triangle ABC$ similar to $\triangle AED$?
Note: The figure is not necessarily drawn to scale.
\Box Yes, triangle $\triangle ABC$ is similar to $\triangle AED$?
\Box No, triangle $\triangle ABC$ is not similar to $\triangle AED$?

General Strategies:

- 1. Read the problem.
- 2. Highlight key words.
- Identify the math topics.
- 4. Re-read the problem.
- Define your steps (your game plan) – this is criteria 3.
- 6. Refer to your memory aid, as needed.
- 7. Solve.
- If you get stuck on a calculation, pick a number and keep going.
- 9. Ask yourself whether your answer makes sense.
- 10. Write your answer statement.

Show any or all your work! Do not leave a blank page!



Khan Academy video: <u>http://www.khanacademy.org/math/geometry/similarity/triangle</u> <u>similarlity/v/similarity-postulates</u> Similarity postulates

Explore Learning Gizmos, <u>http://www.explorelearning.com/</u> look up Similarity in Right Triangles

3.3 Metric Relations (Right Triangles)

The following information about triangle ABC below is known:

- m∠ABC = 90°
- \overline{BD} is an altitude
- m \overline{AB} = 60 m
- m \overline{BC} = 80 m



What is the measure of altitude \overline{BD} ?

- A) 36 m
- B) 48 m
- C) 64 m
- D) 69 m

General Strategies:

- 1. Read the question.
- 2. Highlight key words.
- Identify the math topic.
- 4. Re-read the question.
- 5. Refer to your memory aid, as needed.
- Solve the problem without looking at choices shown (A, B, C and D).
- 7. Look at all the choices.
- Match your answer to the appropriate choice.

Do not leave a blank! Make a choice!

Г

Answer and Solution:	Suggested Strategies:	
Step 1: Pythagorean Theorem	 Put the measures onto the diagram. 	
$(m\overline{AC})^2 = 60^2 + 80^2$	2) If you are using	
$m\overline{AC} = \sqrt{3600 + 6400}$	formulas, make sure	
$m\overline{AC} = 100 \ m$	you label the triangle according to your formulas	
Step 2: Apply Metric Relation	3) Identify the metricrelation(s) that	
$a \bullet b = c \bullet h$	enable(s) you to solve	
$(m\overline{CB})(m\overline{AB}) = (m\overline{AC})(m\overline{BD})$	for the unknown.	
$60(80) = 100(m\overline{BD})$	4) Consider that it might	
$m\overline{BD} = 4800$	be more than one	
$mbD = \frac{100}{100}$	step.	
$m\overline{BD} = 48 m$	Note: In this case you must apply Pythagorean	
A) 36 m - this is $m\overline{AD}$	applying a metric relation	
	formula.	
B) 48 m - correct		
C) 64 m - this is $m\overline{DC}$		
D) 69 m - this is the result from using an incorrect formula		
The answer is B.		
Additional Resources:		
Visions Volume 1, Section 3.3, p. 181		
Explore Learning Gizmos, <u>http://www.explorelearning.com/</u> look up: si	milarity in right triangles	

Question: General Strategies: Triangle ABC has the following properties: 1. Read the question. 2. Highlight key words. m∠ACB = 90° 3. Identify the math • topic. • \overline{DC} is an altitude 4. Re-read the question. • m \overline{DB} = 45 m 5. Refer to your memory • m \overline{AD} =12 m aid, as needed. 6. Solve the problem without looking at choices shown (A, B, В D C and D). 7. Look at all the choices. 8. Match your answer to the appropriate choice. Do not leave a blank! Make a choice! с **My Strategies:** What is the area of $\triangle ABC$? 139 m^2 A) 523 m² B) 662 m² C) 1325 m² D)

Page 154

Answer and Solution:	Suggested Strategies:	
Step 1: Metric Relation $\begin{aligned} h^2 &= m \cdot n \\ (m\overline{CD})^2 &= (m\overline{AD}) \cdot (m\overline{DB}) \\ m\overline{CD} &= \sqrt{12(45)} \\ m\overline{CD} &= \sqrt{540} \\ m\overline{CD} &= 23.2379 \ meters \end{aligned}$	 Orient the triangle in a way that is easiest for you. Put the measures on the diagram and re- label if necessary. 	
Step 2: Area of Triangle ABC $\frac{m\overline{CD}(m\overline{AD} + m\overline{DB})}{2}$ $\frac{23.2379(12 + 45)}{2}$ $662m^{2}$	 3) Select the appropriate metric relation formula. <i>In this case we need th' and we are given m' and 'n'.</i> 4) Remember your basic area formulas. In this case we need area of triangle. Area = base x height 2 Also be sure you get the area of the requested triangle. In this case the questions ask for triangle ABC – the largest of the three triangles. 	
The answer is C.		
Additional Resources:		
Visions Volume 1, Section 3.3, p. 181 Explore Learning Gizmos, <u>http://www.explorelearning.com/</u> look up: similarity in right triangles		

A construction crane pictured below, has the following measurements:

- $m \angle TWP = 90^{\circ}$
- *VW* is an altitude
- $m\overline{VW} = 50$ metres
- $m\overline{TV}$ = 70 metres



General Strategies:

- 1. Read the question.
- 2. Highlight key words.
- 3. Identify the math topic.
- 4. Re-read the question.
- 5. Make a prediction about the answerwhat will it look like? (an equation, a number, etc.).
- 6. Refer to your memory aid, as needed.
- 7. Solve.
- 8. Ask yourself whether your answer makes sense.
- 9. Write your answer. Do not leave a blank!

My Strategies:

What is the measure of angle WPV to the nearest tenth of a degree?

The measure of angle WPV is _____.



Triangle ABC has the following properties:

- m∠BCA = 90°
- \overline{CD} is an altitude
- m \overline{AB} = 20 m
- m \overline{BC} = 10 m



What is the measure of \overline{AD} ?

The measure of \overline{DA} is _____.

General Strategies:

- 1. Read the question.
- 2. Highlight key words.
- Identify the math topic.
- 4. Re-read the question.
- Make a prediction about the answerwhat will it look like? (an equation, a number, etc.).
- 6. Refer to your memory aid, as needed.
- 7. Solve.
- 8. Ask yourself whether your answer makes sense.
- 9. Write your answer. Do not leave a blank!



A group of Brazilian soccer players are practicing their passes before a game. Their coach illustrates on a Cartesian plane a possible game scenario by showing the players as vertices of three similar right angle triangles.



The coach places the player Zico on the sideline (*y*-axis) to perform a throw-in to the player Kaka, who would pass the ball to Pele located at the coordinates (15, 60) followed by a pass to Falcao located at (60, 90). Units are in meters.

What is the total combined distance of all three passes?

General Strategies:

- 1. Read the problem.
- 2. Highlight key words.
- Identify the math topics.
- 4. Re-read the problem.
- Define your steps (your game plan) – this is criteria 3.
- 6. Refer to your memory aid, as needed.
- 7. Solve.
- If you get stuck on a calculation, pick a number and keep going.
- 9. Ask yourself whether your answer makes sense.
- 10. Write your answer statement.Show any or all your

work! Do not leave a blank page!

My Strategies:

The total combined distance is ______ meters.

Answer and Solution:		Suggested Strategies:	
Step 1: Solve $m\overline{PF}$ Distance formula $\sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$ P(15, 60) and F(60, 90) $\sqrt{(60 - 15)^2 + (90 - 60)^2}$ $m\overline{PF} = \sqrt{45^2 + 30^2} = 5$ Step 2: Solve $m\overline{ZP}$ Set-up equation of line ZF $y = ax + b$ Given P(15, 60) and F(60, 90) $a = \frac{y_2 - y_1}{x_2 - x_1} = \frac{90 - 60}{60 - 15} = \frac{30}{45} = \frac{2}{3}$ $y = \frac{2}{3}x + b$ Now we have to solve for 'b'.	= <i>m</i> P <i>F</i> 4.08	1) We know we have to find distances of three line segments. Line segment \overline{PF} can be found with the distance formula since we are given the coordinates of point P and point F.	
Solve for 'b' by substituting the coordinates of a poin In this case we have a choice between point P and F. you choose. Using the coordinates of point P we have, $60 = \frac{2}{3}(15) + b$ 60 = 10 + b b = 50	t on the line into the equation. It does not matter which one This is the y-coordinate of point Z	2) We know Point Z is on the y-axis. This means the x-coordinate is zero. To solve for the y-coordinate we can set up an equation of a line.	
Step 3: Solve $m\overline{ZP}$ Distance formula $\sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$		y = ax + b	
Z(0, 50) and P(15, 60) $\sqrt{(15-0)^2 + (60-50)^2} = m\overline{PZ}$ $m\overline{PZ} = \sqrt{15^2 + 10^2} = 18.03$		represents the slope $\frac{y_2 - y_1}{x_2 - x_1}$ and 'b' represent the <i>v</i> -intercept.	
Step 4: Metric Relations to solve $m\overline{PK}$ $h^2 = m \cdot n$ $(m\overline{PK})^2 = (m\overline{ZP})(m\overline{PF})$ $m\overline{PK} = \sqrt{18.03(54.08)}$ $m\overline{PK} = 31.22$,	
Step 5: Solving for m \overline{ZK} $m\overline{ZK} = \sqrt{(m\overline{ZP})^2 + (m\overline{R})^2}$ $m\overline{ZK} = \sqrt{18.03^2 + 31.2}$ $m\overline{ZK} = 36.06$			
Step 6: Sum up the lengths of three line segments $m\overline{ZK} + m\overline{PK} + m\overline{PF} = 121.3$			
The total combined distance is 121.37 meter			
Additional Resources:			
Visions Volume 1, Section 3.3, p. 181			

Explore Learning Gizmos, http://www.explorelearning.com/ look up: similarity in right triangles

A group of engineers is planning the construction of the new Champlain Bridge in Montreal. Below is a diagram of a section of the bridge.

The bridge's towers (\overline{BD} and \overline{EC}) are each 100 meters in height and one of the support cables (AB) measures 110 meters.

Also, m \angle ABC and m \angle DEF are both 90° and the towers are perpendicular to the base of the bridge.



To the nearest whole number, what is the length of the cable represented by segment DE?

General Strategies:

- 1. Read the problem.
- 2. Highlight key words.
 3. Identify the math topics.
- 4. Re-read the problem.
- Define your steps (your game plan) – this is criteria 3.
- 6. Refer to your memory aid, as needed.
- 7. Solve.
- If you get stuck on a calculation, pick a number and keep going.
- 9. Ask yourself whether your answer makes sense.
- 10. Write your answer statement.

Show any or all your work! Do not leave a blank page!

My Strategies:

The length of the cable represented by \overline{DE} is_____m.



4.1 Real Functions

Question:	General Strategies:
In a laboratory, scientists are recording the growth rate of cells. They report that a sample of 50 cells doubled every hour.	 Read the question. Highlight key words. Identify the math
Which of the following rules describes the relationship?	topic.
A) $f(x) = 50(x^2)$	 4. Re-read the question. 5. Refer to your memory aid. as needed.
B) $f(x) = 50(2^x)$	6. Look carefully at each
C) $f(x) = 50 + 2x$	B, then C and then D).
D) $f(x) = 2(50^x)$	 B, then C and then D). 7. Eliminate options you know to be incorrect. 8. Solve/check each possible choice. 9. Select the choice that makes the most sense. Do not leave a blank! Make a choice! My Strategies:

Ans	wer and Solution:			Specific Strategies:
	x (number of hours) 0 1 2 3	f(x) (total number of cells) 50 50 x 2 = 100 100 x 2 = 200 200 x 2 = 400		 Since the choices are different function rules; the goal of the problem is to translate the situation into a functional model. Make a table of values to get a clearer picture
An ir	nitial amount which increa	ases by the same multiplie	r is an	of the relation
expo	onential function	<i>f(x)</i> = a(c ^x)		 Doubling the number of cells means you must multiply by 2 for
A)	$f(x) = 50(x^2)$ Since we see the term polynomial function.	x^2 , this is a quadratic or se	cond-degree	 Look on your memory aid for the rule of an
B)	f(x) = 50(2 ^x) This is an exponential a base of 2, which me increase in <i>x.</i>	function with an initial va ans that it is multiplying b	lue of 50 and y 2 for each	exponential function
C)	f(x) = 50 + 2x This is a linear function since we see no expon	n or first-degree polynomia ents.	l function	
D)	f(x) = 2(50 ^x) This is an exponential base are switched.	function, but the initial val	ue and the	
The	answer is B.			
Add	litional Resources:			
Visions Volume 2, Section 4.1, p. 17 (Families of Functions) Visions Volume 2, Section 4.3, p. 39 (Exponential Functions) Explore Learning Gizmos, <u>http://www.explorelearning.com/</u> look up: Exponential functions – Activity A				

A small town in Quebec already received 120 mm of rain this year when a severe storm occurred. During the storm, rain fell at a constant rate of 5 mm per hour.

The graphs below relate the number of hours since the storm began with the accumulated rainfall in mm.

Which graph below correctly illustrates the relationship?



General Strategies:

- 1. Read the question.
- 2. Highlight key words.
- Identify the math topic.
- 4. Re-read the question.
- 5. Refer to your memory aid, as needed.
- Look carefully at each choice shown (A, then B, then C and then D).
- 7. Eliminate options you know to be incorrect.
- 8. Solve/check each possible choice.
- Select the choice that makes the most sense.

Do not leave a blank! Make a choice!

Answer and Solution:

- A) This option is a step function, which means that the amount of rain accumulated remains constant for a period of time and jumps abruptly at critical values; it does not make sense to represent a constant increase of 5mm per hour
- B) This option is a linear function of first-degree polynomial function. It's initial value is 120 and it has a positive slope, indicating a constant increase
- C) This option does not illustrate a constant increase; the amount of rain increases sharply at first, then accumulates more slowly
- D) This option appears to be an exponential function, which would mean that the amount of rain increases by some multiplying factor instead of a constant rate

Specific Strategies:

Since the choices are graphs, this is a problem that can be answered by observation; no calculations need to be done.

- Consider all the functional models on your memory aid
- The linear function model is the only one which offers an interpretation for a constant increase over time

The answer is B.

Additional Resources:

Visions Volume 1, Section 1.2, p. 22 (Lines in the Cartesian Plane) Visions Volume 2, Section 4.1, p. 17 (Families of Functions) Khan Academy video: <u>http://www.khanacademy.org/math/algebra/algebra-functions/</u> <u>relationships_functions/v/basic-linear-function</u> Ex. Constructing a Function

The graph below illustrates a piecewise function whose domain is [0, +∞[. 2-1.5 0.5 0 0.5 1.5 2 2.5 0 Which of the following statements is TRUE? A) The function has no *x*-intercept. B) The function has no y-intercept. C) The function is negative over the interval [0.5, 1.5]. The function has no extrema. D)

Question:

General Strategies:

- 1. Read the question.
- 2. Highlight key words.
- 3. Identify the math topic.
- 4. Re-read the question.
- 5. Refer to your memory aid, as needed.
- 6. Look carefully at each choice shown (A, then B, then C and then D).
- 7. Eliminate options you know to be incorrect.
- 8. Solve/check each possible choice.
- 9. Select the choice that makes the most sense.

Do not leave a blank! Make a choice!

My Strategies:

3



analyzing functions/v/when-a-function-is-positive-or-negative



Answer and Solution:		Suggested Strategies:
A)	The x only has a coefficient so this is a linear function and would be a line.	 Compare the graph of the functions
B)	Correct - The x is an exponent so this is an exponential function and would curve up (or down) sharply and cross the y-axis.	corresponding rules, to the ones provided in the question.
C)	The x is squared so this is a quadratic function and would be a U-shape.	
D)	The x is a denominator so this is an inverse (rational) function and, in this particular case, would not cross the y-axis (since x≠0).	
The a	nswer is B.	
Addit	tional Resources:	
Visions Volume 2, Section 4.1, p. 17 (Families of Functions) Visions Volume 2, Section 4.3, p. 39 (Exponential Functions) Khan Academy video; <u>http://www.khanacademy.org/math/trigonometry/exponential and</u> <u>logarithmic func/exp growth decay/v/exponential-growth-functions</u> – Exponential grown functions		


Answer and Solution:	Specific Strategies:
Answer and Solution: The range is the set of all possible values of y from least to greatest (bottom to top). The lowest value on the graph is y = 0 but this point is an open circle (and therefore not included) and the greatest value on the graph is y = 25. Therefore, the range is]0, 25].	Specific Strategies: Look for the lowest value of y on the graph and the highest value of y on the graph. Use interval notation in providing your answer. (Remember that the smallest value comes first.)
Answer: The range of the function is]0, 25].	
Additional Resources:	
Visions Volume 2, Section 4 (Revision), p. 7 (Properties of Functions)	

A yard and garden care contractor has developed a mathematical model to determine the price he will charge his clients throughout the season. In order to get his clients interested in his service, he gradually increases his price per hour as the hours accumulate.

He illustrates this model in the graph below.



The first piece of the function is a second-degree polynomial function given by the following rule:

 $g(x) = 10x^2$ where $0 \le x \le 8$

The price will remain constant for the next 4 hours but after 12 hours, the contractor charges a flat rate of \$250 for every four hours of work or part thereof.

One client is charged \$1640.

What are the possible numbers of hours that job would have taken?

That job would have taken between _____ and _____ hours.

General Strategies:

- 1. Read the problem.
- 2. Highlight key words.
- Identify the math topics.
- 4. Re-read the problem.
- Define your steps (your game plan) – this is criteria 3.
- 6. Refer to your memory aid, as needed.
- 7. Solve.
- If you get stuck on a calculation, pick a number and keep going.
- 9. Ask yourself whether your answer makes sense.
- Write your answer statement.
 Show any or all your

work! Do not leave a blank page!

Answer and Solution:

Determine the y-value when x = 8 for the function g(x)

 $g(8) = 10(8)^2$

BEDMAS: Remember to apply the exponent first

g(8) = 10 x 64 = 640

So, the step function begins at a y-value of \$640 after 8 hours of work. The price doesn't go up until 12 hours.

<i>x</i> (Number of hours)	;) y (Cost \$)	
[8, 12[\$640	
[12, 16[\$640 + 250 = \$890	
[16, 20] \$890 + 250 = \$114		
[20, 24[\$1140 + 250 = 1390	
[24, 28] \$1390 + 250 = \$164		

For \$1640, it will take 24 to 28 hours, not including 28 hours.

Specific Strategies:

- The first unknown that needs to be determined is the cost for 8 hours of work
- Make sure to keep your work organized from this point – a table is a great idea
- According to the step function, the open circle at x = 12 is a critical value, so the cost will "jump" starting at 12 hours

That job would have taken between 24 and 28 hours.

Additional Resources:

Visions Volume 2, Section 4.1, p. 17 (Families of Functions) Visions Volume 2, Section 4.2, p. 28 (Second-degree Polynomial Function)

Visions Volume 2, Section 4.3, p. 53 (Piecewise Function)

Step Graphs: <u>http://www.youtube.com/watch?v=LUshzsvoGZU</u>

4.2 Second-Degree Polynomial Function

Consider the following function:

$$f(x) = 2x^2$$

B)

Which of the following graphs represents the function?

2









-2



General Strategies:

- 1. Read the question.
- 2. Highlight key words.
- Identify the math topic.
- 4. Re-read the question.
- 5. Refer to your memory aid, as needed.
- Look carefully at each choice shown (A, then B, then C and then D).
- 7. Eliminate options you know to be incorrect.
- 8. Solve/check each possible choice.
- 9. Select the choice that makes the most sense.

Do not leave a blank! Make a choice!



Which rule represents the following graph?



- A) $y = 0.25x^2$
- B) $y = -0.25x^2$
- C) $y = -0.25^x$
- D) y = 0.25x + 1

General Strategies:

- 1. Read the question.
- 2. Highlight key words.
- Identify the math topic.
- 4. Re-read the question.
- 5. Refer to your memory aid, as needed.
- Look carefully at each choice shown (A, then B, then C and then D).
- 7. Eliminate options you know to be incorrect.
- 8. Solve/check each possible choice.
- 9. Select the choice that makes the most sense.

Do not leave a blank! Make a choice!



Consider the following table of values for a quadratic function.

x	f(x)	
- 5	7.5	
0	0	
5	7.5	
10	30	
15	67.5	
20	120	

Which of the following rules represents the quadratic function?

- A) $f(x) = -3x^2$
- B) $f(x) = -0.3x^2$
- C) $f(x) = 0.3x^2$

$$f(x) = 3x^2$$

General Strategies:

- 1. Read the question.
- 2. Highlight key words.
- Identify the math topic.
- 4. Re-read the question.
- 5. Refer to your memory aid, as needed.
- Look carefully at each choice shown (A, then B, then C and then D).
- 7. Eliminate options you know to be incorrect.
- 8. Solve/check each possible choice.
- 9. Select the choice that makes the most sense.

Do not leave a blank! Make a choice!

Answer and Solution:		Suggested Strategies:	
A)	$f(x) = -3x^2$ This function opens down (decreases after the vertex) but the table of values increases after the vertex	 See what patterns you notice among the data. Symmetry around (0,0) 	
B)	$f(x) = -0.3x^2$ This function opens down (decreases after the vertex) but the table of values increases after the vertex	 (0,0) is a minimum so the "a" value will be positive. Since you are told 	
C)	$f(x) = 0.3x^2$ This function opens up and when a non-zero x-value is tested, it gives the corresponding value for f(x): $f(5) = 0.3(5)^2 = 0.3 \times 25 = 7.5$	it is quadratic, you know it's in the form ax^2 so you can calculate a.	
D)	$f(x) = 3x^2$ This function opens up but when a non-zero x-value is tested, it doesn't give the corresponding f(x). $f(5) = 3(5)^2 = 3 \times 25 = 75 \neq 7.5$	Test the two positive functions to see	
OR		which one works.	
Calcula	ate parameter "a" algebraically using one of the points given:		
	$f(x) = ax^2$		
for exa	ample: (5, 7.5) $ \frac{7.5}{25} = \frac{a \times 25}{25} $ $ 0.3 = a$		
The an	iswer is C.		
Additional Resources:			
Visions Volume 2, pp. 28-29 Khan Academy video: <u>https://www.khanacademy.org/math/algebra/quadratics/solving_graphing</u>			

_quadratics/v/graphing-a-quadratic-function http://www.purplemath.com/modules/grphquad.htm

Explore Learning Gizmos, <u>http://www.explorelearning.com/</u> look up: Quadratics in Polynomial Form- Activity A and Activity B (for these, you must keep the b and c sliders at position 0)

Point P (5, 10) is on the curve of the 2nd degree function below.

What is the rule of the function?



General Strategies:

- 1. Read the question.
- 2. Highlight key words.
- Identify the math topic.
- 4. Re-read the question.
- Make a prediction about the answerwhat will it look like? (an equation, a number, etc.).
- 6. Refer to your memory aid, as needed.
- 7. Solve.
- 8. Ask yourself whether your answer makes sense.
- 9. Write your answer.

Do not leave a blank!

My Strategies:

The rule of the function is

Answer and Solution:	Specific Strategies:		
The rule for a second degree function is the form $y = ax^2$ Use the coordinates (5, 10) in the function form to determine parameter "a".	Recall the rule for the second degree function with vertex at the origin is $y = ax^2$.		
$y = ax^{2}$ (10) = a(5) ² 10 = 25a $\frac{10}{25} = \frac{25a}{25}$ $\frac{2}{5}$ or 0.4 = a $y = 0.4x^{2}$ or $f(x) - 0.4x^{2}$	Remember that in any algebraic equation, if you substitute known values, you can solve for the unknown remaining. ASK YOURSELF: What information is given in the graph? An (<i>x</i> , <i>y</i>) point is given in the graph. If you substitute <i>x</i> & <i>y</i> , then only parameter "a" will remain to be determined.		
The rule of the function is $y = 0.4x^2$ or $f(x) = 0.4x^2$			
Additional Resources:			
 Visions Volume 2, pp. 28-29 Explore Learning Gizmos, <u>http://www.explorelearning.com/</u> look up: Quadratic Functions Quadratics in Polynomial Form- Activity A and Activity B (for these, you must keep the b 			

and c sliders at position 0)

Match the second degree functions to their respective graphs.



Function	Graph
A) $y = 5x^2$	
B) $y = -0.2x^2$	
C) $y = x^2$	
D) $y = -x^2$	

General Strategies:

- 1. Read the question.
- 2. Highlight key words.
- Identify the math topic.
- 4. Re-read the question.
- Make a prediction about the answerwhat will it look like? (an equation, a number, etc.).
- 6. Refer to your memory aid, as needed.
- 7. Solve.
- 8. Ask yourself whether your answer makes sense.
- 9. Write your answer.

Do not leave a blank!

Answer and Solution:

Function	Graph
E) $y = 5x^2$	g
F) $y = -0.2x^2$	h
G) $y = x^2$	f
H) $y = -x^2$	k

Suggested Strategies:

- Remember what effect parameter "a" has on the curve:
 - Positive opens up
 - Negative opens down
 - The larger the absolute value of "a" the narrower the curve

Additional Resources:

Visions Volume 2, Section 4.2, pp. 28-29

Explore Learning Gizmos, <u>http://www.explorelearning.com/</u> look up: Quadratics in Polynomial Form- Activity A and Activity B (for these, you must keep the b and c sliders at position 0)

Gordon is responsible for repairing the soccer field. He needs to purchase a square piece of turf that measures 22.5 m by 22.5 m. He finds the following 2 deals from two different companies:

Company A:

The turf is sold in square pieces and the price is calculated according to its area.

Examples of Cost Based on the Rule Using Length of Side

Side length of turf piece	gth of turf iece Cost	
10 m	\$ 1 800	
17 m	\$ 5 202	
25 m	\$11 250	

Company B:

The turf is also sold by area but the pieces are not necessarily square.



Gordon will buy the piece of turf from the company with the lowest price.

How much will Gordon pay for the piece of turf?

General Strategies:

- 1. Read the problem.
- 2. Highlight key words.
- Identify the math topics.
- 4. Re-read the problem.
- Define your steps (your game plan) – this is criteria 3.
- 6. Refer to your memory aid, as needed.
- 7. Solve.
- Ask yourself whether your answer makes sense.
- 9. Write your answer statement.

Show any or all your work! Do not leave a blank page!

Answer and Solution:	Suggested Strategies:	
Company A:	Company A:	
You can use any of the points to substitute them in $y = ax^2$ $y = ax^2$ Let x be the length of side $(1800) = a(10)^2$ 1800 = 100a $\frac{1800}{100} = \frac{100a}{100}$ a = 18 rule : $y = 18x^2$ Now that you have the rule, you can substitute accordingly: Turf piece of 22.5m (x value): $y=18 \times (22.5)^2$ y=9112.5 \$9 112.50	Turf is sold in SQUARE pieces and the cost depends on the AREA (s ²) ASK YOURSELF: Which kind of function is associated with squaring a number? $y = ax^2$ Substitute (x, y) value and solve for "a". This will give you your rule and you can then substitute and solve for y. Company B:	
Company B:Calculate the area of the square piece of turf: $22.5 \times 22.5 = 506.25 m^2$ Reading the graph, you can see that $506.25 m^2$ corresponds to a cost of \$11 000.Gordon will buy the turf at the lowest price and therefore he will buy from Company A.Gordon will pay \$9 112.50 for the turf.	Before you can use this graph, you need to calculate the area of the turf Gordon needs.	
Additional Resources: Visions Volume 2, pp. 28-29 Khan Academy video: <u>https://www.khanacademy.org/math/algebra/quadratics/solving_graphing_quadratics/v/graphing-a-quadratic-function</u> <u>http://www.purplemath.com/modules/grphquad.htm</u> Explore Learning Gizmos, <u>http://www.explorelearning.com/</u> look up: Quadratics in Polynomial Form- Activity A and Activity B (for these, you must keep the b and c sliders at position 0)		

4.3 Exponential Function

A house, initially valued at \$275 000, increases in value by 2% annually.

Let:

- x : represent the number of years and
- f(x): represent the value of the house,

Which of the following equations defines this situation?

A)	$f(x) = 275\ 000\ (0.02)^{x}$
•••)(,,) = 2 = 2 = 2 = 2 = 2 = 2

B) $f(x) = 275\ 000\ (1.02)^x$

- C) $f(x) = 275\ 000\ (1.2)^x$
- D) $f(x) = 275\ 000(0.98)^x$

General Strategies:

- 1. Read the question.
- 2. Highlight key words.
- Identify the math topic.
- 4. Re-read the question.
- Make a prediction about the answerwhat will it look like? (an equation, a number, etc.).
- 6. Refer to your memory aid, as needed.
- 7. Solve.
- 8. Ask yourself whether your answer makes sense.
- 9. Write your answer. Do not leave a blank!

Answer and Solution:		Suggested Strategies:		
Expone f(x) = a where	ential Function: u(c) ^x : <i>a</i> is the initial value and <i>c</i> is the base	 Find the type of function for the situation. Calculate "c" by 		
Given	the value increases, $C > 1$	 using the percentage. Remember that in growth situations we add to 100%. 		
2/100	= 0.02 and then adding it to 1			
C = 100	0% + 2% = 102% = 1.02			
The co	rrect equation is $f(x) = 275\ 000\ (1.02)^{x}$			
A)	$f(x) = 275\ 000\ (0.02)^x$ This would be a decreasing function since the base is less than 1.			
B)	<i>f</i> (<i>x</i>) = 275 000 (1.02) ^x This is correct.			
C)	$f(x) = 275\ 000\ (1.2)^{x}$ m This would represent a growth rate of 20% not 2%.			
D)	<i>f</i> (<i>x</i>) = 275 000(0.98) ^x This would represent a decay of 2% (decreasing).			
The an	iswer is B.			
Additional Resources:				
Visions	Visions Volume 1, pp. 39-41			

Given the exponential function $f(x) = 505 (0.94)^x$, Where,

x : represent the numbers of years since 2010

f(x) : represent the cost of the bike

Which of the following statements is true?

- A) The initial value is 0.94.
- B) The bike's value decreases by 94% yearly.
- C) The function is increasing.
- D) In the year 2020, the value of the bike will be \$272.

General Strategies:

- 1. Read the question.
- 2. Highlight key words.
- Identify the math topic.
- 4. Re-read the question.
- Make a prediction about the answerwhat will it look like? (an equation, a number, etc.).
- 6. Refer to your memory aid, as needed.
- 7. Solve.
- 8. Ask yourself whether your answer makes sense.
- 9. Write your answer. Do not leave a blank!

Answer and Sol	ution:	Sugg	ested Strategies:	
The initial value is 505, not 0.94.		•	• Determine what the	
The bike's value decreases by 6%, not 94%.			initial value is and compare with A).	
This is a decreasing	g function because 0.94 is less than 1.	• Determine the percentage decrease		
The value of the bike will be \$272 in the year 2020. Proof: 2020 - 2010 = 10 years $f(10) = 505(0.94)^{10} = 272$		•	and compare with B). Determine if the function is increasing and compare with C)	
A) The initial v No – the in	value is 0.94. itial value is \$505.	•	Calculate the number of years from 2010 to 2020 and replace value in	
B) The bike de	creases by 94% yearly.		<i>x</i> . Compare with D).	
No – the ra	te at which it decreases is 1 – 0.94 = 0.06, or 6%			
C) The graph i No – since	s an increasing function. the base is less than one, it is a decreasing function.			
D) In the year	2000, the value of the bike will be \$272. Yes:			
2000 – 199 f(10) = 505 The answer is D.	0 = 10 years (0.94) ¹⁰ =272			
Additional Resources:				
Visions Volume 1, pp. 39-41				

The value of a video game depreciates 35% yearly. In 5 years, the price of the video game will be \$10.21.

What is the initial price of the video game?

General Strategies:

- 1. Read the question.
- 2. Highlight key words.
- Identify the math topic.
- 4. Re-read the question.
- Make a prediction about the answerwhat will it look like? (an equation, a number, etc.).
- 6. Refer to your memory aid, as needed.
- 7. Solve.
- 8. Ask yourself whether your answer makes sense.
- 9. Write your answer. Do not leave a blank!

My Strategies:

The initial price of video game is ______.

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Answer and Solution:	Suggested Strategies:
$f(x) = ac^{x}$ $c = 1 - 0.35 = 0.65$ $f(x) = a (0.65)^{x}$ $10.21 = a (0.65)^{5}$ $\frac{10.21}{0.1160} = \frac{0.1160}{0.1160}$ $a = 88.02	 Notice that this is an exponential function that is decreasing. Write the equation for this function. Calculate the value of "c" which uses the percentage. Fill in x with the number of years and y with the price after 5 years. Work backwards to find <i>a</i>, the initial price. Remember that in decay or decreasing situations we subtract from 100%.
Additional Resources:	
Visions Volume 1, pp. 39-41	

Question:	General Strategies:
The function f described below represents the number of bacter a well, in relation to the amount of time elapsed since 2005. $f(x) = 4500 (1.33)^x$ where: x is the number of years elapsed since 2005 f(x) is the number of bacteria In what year will the number of bacteria be 137 858?	 ria in 1. Read the question. 2. Highlight key words. 3. Identify the math topic. 4. Re-read the question. 5. Make a prediction about the answerwhat will it look like? (an equation, a number, etc.). 6. Refer to your memory aid, as needed. 7. Solve. 8. Ask yourself whether your answer makes sense. 9. Write your answer. Do not leave a blank! My Strategies:
In the number of bacteria will be 137 858.	

Answer and Solution:	Suggested Strategies:
OR $x 4500(1.33)^{x} f(x)$ $1 4500(1.33)^{1} 5985.0$ $2 4500(1.33)^{2} 7960.1$ $3 4500(1.33)^{3} 10586.9$ $4 4500(1.32)^{4} 41020.5$	 Replace y by the number of bacteria given. Work backwards to find the value of x by guess and check.
A 4500(1.33) ² 14080.5 5 4500(1.33) ⁵ 18727.1 6 4500(1.33) ⁶ 24907.1 7 4500(1.33) ⁷ 33126.4 8 4500(1.33) ⁸ 44058.1 9 4500(1.33) ⁹ 58597.3 10 4500(1.33) ¹¹ 77934.4 11 4500(1.33) 137858.1 13 4500(1.33) ¹¹ 183351.2 x = 12 years later 2005 + 12 = 2017 Answer: In 2017 the number of bacteria will be 137 858.	 Set up a table of values for the function and find the <i>y</i> value you are looking for. In the table, you can jump ahead to where you think <i>x</i> would work. Your table should contain more than two calculations in order to show evidence of your thinking.
Additional Resources:	1
Visions Volume 1, pp. 39-41	

Question:	General Strategies:
Sophia invested \$5000 today. Her investment will increase by 2.5% each year. How much profit will she have made in 10 years?	 Read the question. Highlight key words. Identify the math topic. Re-read the question. Make a prediction about the answer- what will it look like? (an equation, a number, etc.). Refer to your memory aid, as needed. Solve. Ask yourself whether your answer makes sense. Write your answer. Do not leave a blank!
	My Strategies:
Sophia will have made profit in 10 years.	

Answer and Solution:	Suggested Strategies:
$f(x) = ac^{x}$ a = initial value = 5000 (principal) c = growth rate = 1 + 0.025 = 1.025 OR 100% + 2.5% = 102.5% or 1.025 $f(x) = 5000 (1.025)^{x}$ where: x is the number of years and $f(x) = 5000 (1.025)^{10}$ f(x) = \$6400.42 6400.42 - 5000 = \$1400.42	 Notice this is an exponential function and that it is increasing so the base is greater than 1. Write the equation associated with the function. Substitute the initial value for "a". Determine "c" by using the percentage. Recognize that x represents the number of years and y represents the total amount. Plug in number of years for "x".
Answer: Sophia will have made \$1400.42 profit in 10 years.	
Additional Resources:	
Visions Volume 1, pp. 39-41	

Amy and Ben have deposited money in different banks.

Amy initially deposited \$400 in the bank, and deposits \$10 into her account every month. No interest is earned.

Ben made a one-time investment of \$850 at a yearly interest rate of 4%.

Who will have more money saved after 5 years?

General Strategies:

- 1. Read the question.
- 2. Highlight key words.
- 3. Identify the math topic.
- 4. Re-read the question.
- Make a prediction about the answerwhat will it look like? (an equation, a number, etc.).
- 6. Refer to your memory aid, as needed.
- 7. Solve.
- 8. Ask yourself whether your answer makes sense.
- 9. Write your answer. Do not leave a blank!

My Strategies:

_ will have more money after 5 years.

Answer and Solution:	Suggested Strategies:
Amy: f(x) = 10x + 400 where: x is the number of months f(x) is the total amount of money in the bank After 5 years (5 x 12 = 60 months), the total amount is: f(60) = 10(60) + 400 = \$1000 Ben: $f(x) = 850(1.04)^x$ where: x is the number of years f(x) is the total amount of money in the bank After 5 years, the total amount is: $f(5) = 850(1.04)^5 = 1034.15 The person who will have the most money after 5 years is Ben.	 Find the function representing Amy & Ben's situation. If the function is linear then "a" is the amount placed monthly and "b" is the initial amount invested. If the function is exponential then "a" is the amount invested and "c" is calculated by using the percentage given. Replace x in both equations by the amount of years given.
Answer: Ben will have more money after 5 years.	
Additional Resources:	
Visions Volume 1, pp. 39-41	

Question:	General Strategies:
A study examined the populations of four neighboring towns.	 Read the problem. Highlight key words.
<u>Town A</u> In 1960, Town A had 5000 inhabitants. Since then, there has been an equal amount of births as there have been deaths and the number of people moving away has matched the number of people moving to the town.	 Identify the math topics. Re-read the problem. Define your steps (your game plan) – this is criteria 3.
Town BFunction f described below represents the population of Town B in relation to the time elapsed since 2001. $f(x) = 2000 (1.022)^x$ where: x represents time elapsed since 2001, in years $f(x)$ represents the population of Town B	 Refer to your memory aid, as needed. Solve. If you get stuck on a calculation, pick a number and keep going. Ask yourself whether
<u>Town C</u> In 2010, Town C had 5000 inhabitants. The population has decreased by 50 inhabitants every year.	your answer makes sense. 10. Write your answer statement.
<u>Town D</u> In 2006, Town D had a population of 1500. It is estimated that the population will increase by 5% annually.	Show any or all your work! Do not leave a blank page!
The four towns will be merged in 2020 to form one city.	My Strategies:
What will the population of the new city be when it is formed in 2020?	
The population of the new city will be	

Answer and Solution:	Suggested Strategies:
Town A: constant function f(x) = 5000, where: x is the number of years elapsed since 1960 f(x) is the total inhabitants. Town B: exponential function 2020 - 2001 = 19 years elapsed. $f(19) = 2000 (1.022)^{19} = 3024$ inhabitants	 Determine the type of function for each town and write the equation. Determine the number of years that pass between the time of the merging and the
Town C: linear function 2020 - 2010 = 10 years elapsed f(x) = 5000 - 50 (x) f(19) = 5000 - 50 (19) = 4050 inhabitants.	 creation of each town. Replace x by the number of years that pass in each
Town D : exponential function For $c = 100\% + 5\%$ = 105% = 1.05 a = initial population of 1500 $f(x) = ac^x$ $f(x) = 1500 (1.05)^x$ x = 2020 - 2006 = 14 $f(14) = 1500 (1.05)^{14} = 2969$ inhabitants	equation.
Total: 5000 + 3024 + 4050 + 2969 = 15 043 inhabitants	
Answer: The population of the new city will be 15 043.	
Additional Resources:	
Visions Volume 1, pp. 39-41	

4.4 Step, Periodic and Piecewise Functions


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Answer and Solution:		Suggested Strategies:
A) 8	This is the answer you get if you use a scale of 1 instead of 2.	To find the period of a periodic function means that the y values will
B) 16	Correct	repeat over a certain interval of <i>x</i> .
C) 24	This is the answer you get if you use the whole graph and not just one period, and a scale of 1 instead of 2.	The period can also be thought of as the length
D) 48 The answer i	This is the answer you get if you use the whole graph and not just one period.	In this case, the graph starts at 10, goes to 30, and back down to 10. At this point the graph starts repeating. Look at the <i>x</i> values to find the period. In this case the graph repeats after 8 units/squares but each unit is worth 2 so the period is 16 units.
Additional	Resources:	
Visions Volur	ne 2, Section 4.4, p. 53	

A store offers a discount of \$5 for every \$50 in purchases. The graph below illustrates the relation between the value of the purchases and the amount of discount a customer receives.





Consider the following five statements regarding the graph.

- 1. A customer who spends \$150 will receive a \$10 discount.
- 2. A customer who spends \$75 will receive a \$5 discount.
- 3. A customer will receive a \$5 discount when spending less than \$100.
- 4. A customer will receive twice as much of a discount when spending \$200 than \$100.
- 5. A customer will receive no discount when spending less than \$50.

Which of the statements above are true?

- A) 2, 4 and 5
- B) 2, 3 and 4
- C) 1, 2 and 4
- D) 1, 2 and 3

General Strategies:

- 1. Read the question.
- 2. Highlight key words.
- Identify the math topic.
- 4. Re-read the question.
- 5. Refer to your memory aid, as needed.
- Solve the problem without looking at choices shown (A, B, C and D).
- 7. Look at all the choices.
- Match your answer to the appropriate choice.

Do not leave a blank! Make a choice!

Answer and Solution:	Suggested Strategies:
Read each statement carefully.	1) "greatest integer function" is another
1. A customer that spends \$150 will receive a \$10 discount.	name for step function.
False-\$150=\$15 discount	2) Read each statement
2. A customer that spends \$75 will receive a \$5 discount.	determine if it is true or false.
<i>True – In values between the endpoints of the step has the same y-value.</i>	3) When reading the endpoints of the steps
 A customer will receive a \$5 discount when spending less than \$100. 	between an open circle and filled in circle.
False — Be careful with the less than \$100. Less than \$100 includes less than \$50. Less than \$50 equals \$0 discount.	Endpoints
 A customer will receive twice as much of a discount when spending \$200 than \$100. 	 A closed point means it is included.
True – The discount for \$200 = \$20 and \$100= \$10	 An open point means it is not
 A customer will receive no discount when spending less than \$50. 	included.
True – Less than \$50 is the step on the x-axis.	4) The question is looking for the <u>true</u> statements. Sometimes the question wants the <i>false</i> statements. Take a moment to highlight the word <u>true</u> and
The answer is A.	statement as true or false as you read them.
Additional Resources:	1
Visions Volume 2, Section 4.4, p. 53	

Question:	General Strategies:
The cost to park a car in a particularly expensive lot is \$40 for the first half hour and \$5.00 for each additional hour or part thereof. A customer uses this parking lot for five hours.	 Read the question. Highlight key words. Identify the math topic.
How much will the customer pay for parking?	 Re-read the question. Make a prediction about the answer- what will it look like? (an equation, a number, etc.). Refer to your memory aid, as needed. Solve. Ask yourself whether your answer makes sense. Write your answer. Do not leave a blank! My Strategies:
The customer will pay \$ for parking 5 hours.	



Two companies offer different prices for internet service. Company A uses a linear model where each 100 gigabytes of usage will cost \$20. Company B follows a greatest integer function as shown on the graph below.



What is the difference in cost between the two companies for 200 gigabytes?

General Strategies:

- 1. Read the question.
- 2. Highlight key words.
 3. Identify the math topic.
- 4. Re-read the question.
- Make a prediction about the answerwhat will it look like? (an equation, a number, etc.).
- Refer to your memory aid, as needed.
- 7. Solve.
- 8. Ask yourself whether your answer makes sense.
- 9. Write your answer. Do not leave a blank!

My Strategies:

The difference in cost is _____

Answer and Solution:	Suggested Strategies:
Company A: $\frac{100 \ gb}{\$20} = \frac{200 \ gb}{\$x} \to x = \$40$	1) Since we can't read off the graph for the cost of 200 gb from Company A, we need
OR	 The text says each 100 ch costs \$20 cc
We can see the line passing through the origin (0, 0) and the given point (100, 20)	we could set up a proportion or
\$20 per 100 gigabytes \$0.20 per 1 gigabyte	 The graph shows the same information but we can find a
The function rule to calculate the cost in relation to the internet usage (gigabyte) will be $f(x) = 0.20x$	unit rate which will be the " <i>a</i> " in y = ax + b. b will be 0
The cost of 200 gigabyte $f(200) = $ \$40	since the line goes through the origin.
Company B:	Recall: 'a' in the equation represents the slope $\frac{y_2 - y_1}{x_2 - x_1}$
From the graph – f(200) = \$25 (Note that it isn't \$35 because it's the solid dot that indicates the y- value.)	and 'b' represent the y-intercept. (In this case it is 0 since the line passes through the origin.
The difference: \$40 - \$25 = \$15 Answer: The difference in cost is \$15.	2) By looking at the graph we can see the exact value of the cost of Company B at 200 gb. Be careful not to take the \$35 value. Remember the difference between a white circle and a black circle.
Additional Resources:	
Visions Volume 2, Section 4.4, p. 53	

A store selling World Cup memorabilia places a mechanical mascot in front of the store.

The mascot raises a ball from the ground to a maximum height of 150 cm at a constant rate, holds it there for 20 seconds, and then lowers it back to ground level at the same rate.

The graph below illustrates a periodic function that represents the height, or the distance between the ball and the ground in relation to the time elapsed in seconds.



A store employee turns on the mechanism that moves the soccer ball at 8:00AM. At that point the ball is at ground level. At exactly 8:15 AM, the mechanism breaks down and the soccer ball stops moving.

How high above the ground is the ball when the mascot stops moving?

The ball is _____ cm off the ground when the mascot stops moving.

General Strategies:

- 1. Read the problem.
- 2. Highlight key words.
- Identify the math topics.
- 4. Re-read the problem.
- Define your steps (your game plan) – this is criteria 3.
- 6. Refer to your memory aid, as needed.
- 7. Solve.
- If you get stuck on a calculation, pick a number and keep going.
- 9. Ask yourself whether your answer makes sense.
- Write your answer statement.
 Show any or all your work! Do not leave a

blank page!

Answer and Solution:

Step 1: Determine the period of the function

5 complete cycles = 400 seconds 1 complete cycle = 80 seconds

Step 2: Determine how many complete cycles from 8:00-8:15 AM

Since our unit of time on our graph is in seconds we need to convert minutes to seconds.

15 minutes x 60 seconds/minute = 900 seconds

Determine the number of complete cycles in 900 seconds

$$\frac{900 \ seconds}{80 \frac{seconds}{cycle}} = 11.25 \ cycles$$

11 Full Cycles means that the ball will return back to where it started (i.e. ground) 0.25 of a cycle represents quarter of a full cycle. (0.25 x 80seconds = 20 seconds)

OR

The graph (5 cycles) covers 400 seconds, so 800 seconds covers the graph twice, leaving 100 seconds (900 – 800) left over to being the third time. From reading the graph, you can see that at 100 seconds, the ball is 100 cm above the ground. HOWEVER, even though it *looks* like 100, make sure by showing the following:

Step 3: Determine the height the ball is relative to the ground at 20 seconds

To find the exact value we need to break a cycle into pieces.



At 20 seconds the ball will be moving upwards. To know the exact height we will have to find the equation of a line: y = ax + b.

We have two points on the line. $P_1(0,0)$ and $P_2(30,150)$

 $a = \frac{y_2 - y_1}{x_2 - x_1} = \frac{150 - 0}{30 - 0} = \frac{150}{30} = 5$ and b = 0 since the *y*-intercept is at the origin.

The equation of the line is y = 5x

To find the height of the ball at 20 seconds, substitute x=20 and solve for y. y = 5(20) = 100 centimeters

The ball is <u>100</u> cm off the ground when the mascot stops moving.

Additional Resources:

Visions Volume 2, Section 4.4, p. 53

Suggested Strategies:

 Determine the period (the length of a full cycle) of the periodic function.

Note: The scale of x-axis is 100/4 = 25 seconds per grid mark.

In this case you cannot determine the exact value of the period from looking at one cycle on the graph. Instead we can see that 5 full cycles equals 400 seconds.

(1 cycle = 80seconds)

- 2) At 8:00 AM the ball starts at ground level and moves for 15 minutes. We need to figure out how many complete cycles we have completed in 15 minutes and see what's left over.
- 3) Write the equation of a line given two points. y = ax + b

Recall: 'a' in the equation represents the slope $\frac{y_2-y_1}{x_2-x_1}$ and 'b' represent the *y*-intercept.





http://www.mathsisfun.com/sets/functions-piecewise.html http://www.purplemath.com/modules/strtlneq.htm

5.1 Trigonometric Ratios

Consider the right triangle ABC shown below.



Which of the following expressions represents the correct trigonometric ratio for angle A?

A)
$$\sin A = \frac{9}{2}$$

B)
$$\tan A = \frac{9}{2}$$

C)
$$\cos A = \frac{2}{9}$$

D)
$$\tan A = \frac{2}{9}$$

General Strategies:

- 1. Read the question.
- 2. Highlight key words.
- Identify the math topic.
- 4. Re-read the question.
- 5. Refer to your memory aid, as needed.
- Solve the problem without looking at choices shown (A, B, C and D).
- 7. Look at all the choices.
- Match your answer to the appropriate choice.

Do not leave a blank! Make a choice!















In isosceles triangle RST, height QT measures 13.1 cm.



What is the measure of angle R to the nearest tenth?

General Strategies:

- 1. Read the question.
- 2. Highlight key words.
- Identify the math topic.
- 4. Re-read the question.
- Make a prediction about the answerwhat will it look like? (an equation, a number, etc.).
- 6. Refer to your memory aid, as needed.
- 7. Solve.
- 8. Ask yourself whether your answer makes sense.
- 9. Write your answer.

Do not leave a blank!

My Strategies:

The measure of angle R is _____

Answer and Solution:	Specific Strategies:
Opposite side S Q Adjacent side 31 cm	Which angle is given? or unknown? Which sides are given?
 The focus is on triangle TQR Triangle TQR is a right triangle because the height is perpendicular to the base. The measurement of QR is 31 ÷ 2 because the triangle is isosceles Use trigonometric ratios The "knowns" are the opposite side and adjacent side to angle R The correct trigonometric ratio is Tan (TOA) Remember to divide RS by two to obtain the value of the adjacent side of angle R. 31 ÷ 2 = 15.5 tan R = opposite/adjacent 	Looking for an unknown in a right triangle means that you will need to use trigonometric ratios. Remember: SOH CAH TOA 1. Label sides according to the given angle 2. Select the appropriate trigonometric ratio (sin, cos or tan) 3. Solve for the unknown
$ \tan R = \frac{1}{15.5} $ $ R = \tan^{-1} 0.8451 $ $ R = 40.2^{0} $ The measure of angle R is 40.2 ⁰ .	
Additional Resources:	
Visions Volume 2, pp. 84-85 Khan Academy video: <u>https://www.khanacademy.org/math/trigonome</u> <u>basic_trig_ratios/v/exampletrig-to-solve-the-sides-and-angles-of-a-rig</u> <u>http://www.purplemath.com/modules/basirati2.htm</u>	etry/basic-trigonometry/ ght-triangle

Question: In the figure below, triangle BEF and triangle ABC are right triangles.

In addition,

 \overline{DB} is an altitude of right triangle ABC $\overline{AE} \cong \overline{BE}$ $m \angle BEF = 36^{\circ}$ $m \overline{EF} = 15cm$ $m \overline{DB} = 9cm$

The drawing is not to scale.

What is the area of figure AEFC?



General Strategies:

- 1. Read the problem.
- 2. Highlight key words.
 3. Identify the math
- topics.
- 4. Re-read the problem.
- Define your steps (your game plan) – this is criteria 3.
- 6. Refer to your memory aid, as needed.
- 7. Solve.
- If you get stuck on a calculation, pick a number and keep going.
- 9. Ask yourself whether your answer makes sense.
- 10. Write your answer statement.

Show any or all your work! Do not leave a blank page!



5.2 Finding Missing Measurements



Answer and Solution:	Suggested Strategies:
$10 x = \tan x = 28$ $10 x = \tan^{-1}(2.8) = 70.3^{\circ}$ $? = 180^{\circ} - 2(70.3^{\circ})$ $= 39.4^{\circ}$ (You may instead get the result 39.3° which would be correct.) A) Incorrect. Did $\tan x = \frac{10}{28}$ and forgot to subtract from 180° . B) Correct answer. C) Incorrect. Forgot to subtract from 180° . D) Incorrect. Did $\tan x = \frac{10}{28}$ and subtracted from 180° .	 Identify the triangles that you see – two right triangles and an isosceles triangle. Determine if the two right triangles are the same. (they are by SAS – the two legs and the right angles) Since you know the lengths of two sides of the right triangle, you can use a trig ratio to find the angle(s) You know that the sum of the angles along the side of the rectangle measuring 20 must add up to 180. Find <i>x</i> and subtract that twice from 180 and you'll get the measure of the missing angle.
The answer is B.	
Additional Resources:	
Visions Volume 1 p. 95 (Mathematical Knowledge Summary) Explore Learning Gizmos, <u>http://www.explorelearning.com/</u> look up: Proving Sine, Cosine and Tangent Khan Academy video: <u>http://www.khanacademy.org/math/geometry/right_triangles</u> <u>topic/ccgeometry-trig/v/basic-trigonometry</u> Sine, Cosine and Tangent Trigonometric Functions	





Sylvain wants to paint the surface of his triangular deck.

What is the area to be painted?



- A) 87.3 m²
- B) 93.6 m²
- C) 119.4 m²
- D) 137.3 m²

General Strategies:

- 1. Read the question.
- Highlight key words.
 Identify the math
- topic.
- 4. Re-read the question.
- 5. Refer to your memory aid, as needed.
- Solve the problem without looking at choices shown (A, B, C and D).
- 7. Look at all the choices.
- Match your answer to the appropriate choice.

Do not leave a blank! Make a choice!



topic/ccgeometry-trig/v/basic-trigonometry Sine, Cosine and Tangent Trigonometric Functions

Bird nests are sitting at the top of two poles. Pole A is 11.5 m long and is leaning at an 8° angle from the vertical; Pole B is 11 m long and is leaning at a 5° angle from the vertical.

What is the difference in height between the two bird nests?

Give your answer to 2 decimal places.

A 5° B 11.5 m 11 m

General Strategies:

- 1. Read the question.
- 2. Highlight key words.
- Identify the math topic.
- 4. Re-read the question.
- Make a prediction about the answerwhat will it look like? (an equation, a number, etc.).
- 6. Refer to your memory aid, as needed.
- 7. Solve.
- 8. Ask yourself whether your answer makes sense.
- 9. Write your answer. Do not leave a blank!

My	Strategies:	
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The difference in height between the two bird nests is	
--	--

m.



A flagpole is anchored using two guy wires. The guy wire on the right is 18 m long and has an angle of inclination with the ground of 30°. It is attached one meter below the point where the left guy wire is attached to the pole. The left guy wire is located 20 meters from the base of the flagpole.

What is the angle of inclination of the left guy wire?



General Strategies:

- 1. Read the question.
- 2. Highlight key words.
- 3. Identify the math topic.
- 4. Re-read the question.
- Make a prediction about the answerwhat will it look like? (an equation, a number, etc.).
- 6. Refer to your memory aid, as needed.
- 7. Solve.
- Ask yourself whether your answer makes sense.
- 9. Write your answer. Do not leave a blank!

My Strategies:

The angle of inclination of the left guy wire is ____






topic/ccgeometry-trig/v/basic-trigonometry Sine, Cosine and Tangent Trigonometric Functions

General Strategies: 1. Read the problem.

3. Identify the math

5. Define your steps

topics.

2. Highlight key words.

4. Re-read the problem.

(your game plan) -

this is criteria 3.

Question:

Sally is flying a kite. The tip of the kite is 60 m above the ground and the kite itself is 2m in length. She is holding the string 1 m above the ground. The angle of inclination of the string started out at 55° but then the wind shifted and the angle of the string shrunk to 40°. In order to maintain the height of the kite, Sally had to let more string out from the spool.

How much string did Sally need to let out to maintain the height of the kite?



Answer and Solution:	Suggested Strategies:		
Height of kite where the string is attached is 60 m - 2 m = 58 m Sally is holding the string one meter up so height for calculation is 58 -1 = 57 m 2 m 2	 The tricky part of this question is trying to imagine what exactly is happening. From the diagram, you can probably see that triangles are involved; sketch them separately in a way that will make it easier to see how to set up the trig ratios Recognize that the string is the hypotenuse of these triangles and get the feel that the hypotenuse will be longer if the angle is smaller. Now figure out the two lengths and find the difference. 		
Sally had to let out an additional 19 1 m of string to maintain the			
height of the kite.			
Additional Resources:			
Visions Volume 2 p. 95 (Mathematical Knowledge Summary) Explore Learning Gizmos, <u>http://www.explorelearning.com/</u> look up: Proving Sine, Cosine and Tangent Khan Academy video: <u>http://www.khanacademy.org/math/geometry/right_triangles</u> topic/ccgeometry-trig/y/basic-trigonometry Sine. Cosine and Tangent Trigonometric Functions			
topic/cogeometry-trig/v/basic-trigonometry sine, cosine and rangent trigonometric functions			

5.3 Calculating the Area of any Triangle



Answer and Solution:	Specific Strategies:	
$\frac{d}{sinA} = \frac{1}{sinC}$ $\frac{12}{sinA} = \frac{15}{sin98}$ $12(sin98) = 15sinA$	 Notice that this is <u>not</u> a right angle (90⁰) triangle. You <u>cannot</u> apply SOH, CAH, TOA. 	
sinA = 0.79 $A = 52.39^{0}$	 You should use Sine law. 	
A) 52.4°; Correct Answer. B) 38.7°; Did not use sine law, used $\tan CAB = \frac{a}{c}$ instead. C) 53.1°; Did not use sine law, used $\sin CAB = \frac{a}{c}$ instead. D) 36.8°; Did not use sine law, used $\cos CAB = \frac{a}{c}$ instead.	 Color code, highlight or match the angles with their corresponding sides. Apply Sine law formula. 	
I ne answer is A.		
Additional Resources:		
Visions Volume 2, Section 5.3, p. 108 Khan Academy video: <u>https://www.khanacademy.org/math/trigonometry/less-basic-</u> trigonometry/law-sines-cosines/v/law-of-sines Law of Sines		

Consider the following diagram of triangle ABC. All measurements are in meters.



What is the area of triangle ABC?

- A) 7.35 m²
- B) 25.5 m²
- C) 132.3 m²
- D) 187.1 m^2

General Strategies:

- 1. Read the question.
- Highlight key words.
 Identify the math
- topic.
- 4. Re-read the question.
- 5. Refer to your memory aid, as needed.
- Solve the problem without looking at choices shown (A, B, C and D).
- 7. Look at all the choices.
- Match your answer to the appropriate choice.

Do not leave a blank! Make a choice!

My Strategies:

Answ	ver and Solution:	Specific Strategies:	
p :	$= \frac{(a+b+c)}{2}$ $= \frac{(21+18+15)}{2} = 27$	Identify the values of <i>a</i> , <i>b</i> and <i>c</i> according to the diagram provided. Calculate the value of the	
A	$=\sqrt{p(p-a)(p-b)(p-c)}$	half perimeter.	
A A A	$= \sqrt{27(27 - 21)(27 - 18)(27 - 15)}$ = $\sqrt{27(6)(9)(12)}$ = 132.3 m ²	Substitute the values for <i>a</i> , <i>b</i> , <i>c</i> , and <i>p</i> in Hero's formula.	
А	rea = 132.3 m ²		
A)	7.35 m^2 ; added the values under the radical		
B)	25.5 m ² ; Forgot to multiply everything by p under the radical.		
C)	132.3 m ² ; Correct Answer		
D)	187.1 m ² ; Multiplied everything by the perimeter instead of the half perimeter		
The answer is C.			
Additional Resources:			
Visions Volume 2, Section 5.3, p. 108 Khan Academy video: <u>https://www.khanacademy.org/math/geometry/basic-geometry/heron</u>			

formulatutorial/v/ heron-s-formula Heron's Formula

Consider triangle ABC shown below.

What is the measure of angle B. Round your answer to the nearest degree.



General Strategies:

- 1. Read the question.
- 2. Highlight key words.
- 3. Identify the math topic.
- 4. Re-read the question.
- Make a prediction about the answerwhat will it look like? (an equation, a number, etc.).
- 6. Refer to your memory aid, as needed.
- 7. Solve.
- 8. Ask yourself whether your answer makes sense.
- 9. Write your answer. Do not leave a blank!

My Strategies:

The measure of angle B is _____

Answer and Solution:	Specific Strategies:		
Knowing that angle C is 55°, that side C has a length of 10 and side b a length of 7, we can calculate the size of angle B using sine law.	 Notice that this is <u>not</u> a right angle (90⁰) triangle 		
$\frac{a}{sinA} = \frac{b}{sinB} = \frac{c}{sinC}$ To solve the problem, we need three of the four values in any given equality. Since we know b, c and sin C, then: $\frac{b}{sinB} = \frac{c}{sinC}$ Rearranging the equation we get: $\sin B = \frac{bsinC}{c}$ Substituting the corresponding values, we get: $\sin B = \frac{7sin55^{\circ}}{10}$ $\sin B = 0,573406431$ Finding the inverse of sin, sin ⁻¹ , we can get the measure of the angle: $B = \sin^{-1} 0,573406431$ Finding the inverse of sin, sin ⁻² , we can get the measure of the angle: $B = 35^{\circ}$ Answer: Angle B = 35 ⁰	 You <u>cannot</u> apply SOH, CAH, TOA You should use Sine law Color code, highlight or match the angles with their corresponding sides Apply Sine law formula 		
Additional Resources:			
Visions Volume 2, Section 5.3, p. 103 (Activity 1: Sine Law) Khan Academy video: <u>https://www.khanacademy.org/math/trigonometry/less-basic-</u> <u>trigonometry/law-sines-cosines/v/law-of-sines</u> Law of Sines			

What is the area of triangle ABC shown below?



General Strategies:

- 1. Read the question.
- 2. Highlight key words.
- 3. Identify the math topic.
- 4. Re-read the question.
- Make a prediction about the answerwhat will it look like? (an equation, a number, etc.).
- 6. Refer to your memory aid, as needed.
- 7. Solve.
- 8. Ask yourself whether your answer makes sense.
- 9. Write your answer. Do not leave a blank!

My Strategies:

The area of triangle ABC is .

Answer and Solution:	Specific Strategies:	
Before starting with Hero's formula, we must first determine the half- perimeter p of the triangle. $Since p = \frac{(a + b + c)}{2}$ where $a = 7, b = 5$ and $c = 6$ we know that $p = \frac{(7 + 5 + 6)}{2} = 9$ Now using the formula we get: $A = \sqrt{p(p - a)(p - b)(p - c)}$ $A = \sqrt{9(9 - 7)(9 - 5)(9 - 6)}$ $A = \sqrt{9(2)(4)(3)}$ $A = 14.7$ Area = 14.7	Identify the values of <i>a</i> , <i>b</i> and <i>c</i> according to the diagram provided. Calculate the value of the half perimeter. Substitute the values for <i>a</i> , <i>b</i> , <i>c</i> , and <i>p</i> in Hero's formula.	
Additional Resources:		
Visions Volume 2 Activity 2 p. 105 and Mathematical Knowledge p. 108 Khan Academy video: <u>http://www.khanacademy.org/math/geometry/right_triangles_topic/cc-geometry-</u> trig/v/basic-trigonometry Sine, Cosine and Tangent Trigonometric Functions		

Consider triangle ABC shown below. What is the length of segment AB? Round your answer to the nearest tenth.



General Strategies:

- 1. Read the question.
- 2. Highlight key words.
- 3. Identify the math topic.
- 4. Re-read the question.
- Make a prediction about the answerwhat will it look like? (an equation, a number, etc.).
- 6. Refer to your memory aid, as needed.
- 7. Solve.
- Ask yourself whether your answer makes sense.
- 9. Write your answer. Do not leave a blank!

My Strategies:

The length of segment AB is _____

Answer and Solution:	Specific Strategies:		
Knowing that angle B is 53°, that side b has a length of 6 and angle C is 70°, we can calculate the length of side c using sine law. a = b = c	 Notice that this is <u>not</u> a right angle (90⁰) triangle 		
$\frac{a}{sinA} = \frac{b}{sinB} = \frac{c}{sinC}$ To solve the problem, we need three of the four values in any given equality. Since we know b, sin B and sin C, then: $\frac{b}{sinB} = \frac{c}{sinC}$ Rearranging the equation we get: $c = \frac{bsinC}{sinB}$ Substituting the corresponding values, we get: $c = \frac{6sin70^{\circ}}{sin53^{\circ}}$	 You <u>cannot</u> apply SOH, CAH, TOA You should use Sine law Color code, highlight or match the angles with their corresponding sides Apply Sine law formula 		
c = 7.06			
Since side c corresponds to AB, the length of segment AB is 7.06.			
Answer: the length of segment AB is 7.06.			
Additional Resources:			
Visions Volume 2, Section 5.3, p. 103 (Activity 1: Sine Law) Khan Academy video: <u>http://www.khanacademy.org/math/geometry/right_triangles_topic/cc-geometry-trig/v/basic-trigonometry</u> Sine, cosine and tangent trigonometric functions			

The Space Needle is a tall structure in Seattle, Washington. Phil, a math student, attempts to estimate the height of the Space needle by using a clinometer, a device that measures the angle of inclination.



First, Phil stands at point C and reads a 50[°] angle on the clinometer. Then, Phil moves 353 m to Point B and reads an angle of 20[°] on the clinometer. Phil estimates the Space Needle is between 182 m and 188 m in height.

Based on the information given, is Phil's estimation correct? Explain.

□ Yes, his estimation is correct.

 \Box No, his estimation is not correct.

General Strategies:

- 1. Read the problem.
- 2. Highlight key words.
- Identify the math topics.
- 4. Re-read the problem.
- Define your steps (your game plan) – this is criteria 3.
- 6. Refer to your memory aid, as needed.
- 7. Solve.
- If you get stuck on a calculation, pick a number and keep going.
- 9. Ask yourself whether your answer makes sense.
- 10. Write your answer statement.

Show any or all your work! Do not leave a blank page!

My Strategies:



6.2 Subjective Probability and Odds

Which of the following is an example of subjective probability?

- A) You are rolling a die. The probability of rolling a 4 is 1/6.
- B) A camera records the cars passing through an intersection.
 The probability that the next car will be red.
- C) You are waiting for a bus. The probability of it being late is 10%.
- D) You are sitting with your doctor hearing the results of various diagnostic tests. The doctor gives an approximation of your life expectancy.

General Strategies:

- 1. Read the question.
- 2. Highlight key words.
- Identify the math topic.
- 4. Re-read the question.
- Make a prediction about the answerwhat will it look like? (an equation, a number, etc.).
- 6. Refer to your memory aid, as needed.
- 7. Solve.
- Ask yourself whether your answer makes sense.
- 9. Write your answer. Do not leave a blank!

My Strategies:

Answer and Solution:

- A) is theoretical probability.
- B) is experimental/empirical probability.
- C) is experimental/empirical probability.
- D) is subjective probability.

Suggested Strategies:

- Look up the definitions.
- Determine which answer is an example of subjective probability.

The answer is D.

Additional Resources:

Visions Volume 2, p. 152

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Que	estion:	General Strategies:
Wha	at are the odds for rolling a 4 on a fair die?	1. Read the question.
A)	5:1	 Alignlight key words. Identify the math topic.
B)	1:5	4. Re-read the question.
C)	1:6	5. Make a prediction about the answer-
D)	5:6	what will it look like? (an equation, a
		6. Refer to your memory aid, as
		needed.
		 Solve. Ask yourself whether your answer makes sense
		9. Write your answer.
		Do not leave a blank!
		My Strategies:

Answer and Solution:	Suggested Strategies:
"Odds for" is the ratio of favorable outcome to unfavorable outcomes. (favorable : unfavorable)	Determine meaning of "odds for."
Favorable means the outcome you are looking for and unfavorable refers to all other outcomes.	Determine the number of fours you can obtain on a fair
We have one 4 on a die and five other numbers which are not 4, therefore the odds for rolling a 4 are 1:5.	uie.
A) 5:1 odds against rolling a 4	
B) 1:5 odds for rolling a 4	
C) 1:6 probability of rolling a 4	
D) 5:6 probability of not rolling a 4	
The answer is B.	
Additional Resources:	
Visions Volume 2, p. 153	

A boxer has a 30% chance of winning the championship.

What are his odds against winning?

General Strategies:

- 1. Read the question.
- 2. Highlight key words.
- Identify the math topic.
- 4. Re-read the question.
- Make a prediction about the answerwhat will it look like? (an equation, a number, etc.).
- 6. Refer to your memory aid, as needed.
- 7. Solve.
- 8. Ask yourself whether your answer makes sense.
- 9. Write your answer. Do not leave a blank!

My Strategies:

The boxer's odds against winning are _____.

Answer and Solution:	Suggested Strategies:
Answer and Solution: $30\% = \frac{30}{100} = \frac{3}{10} = \frac{favorable}{total}$ Unfavorable = total – favorable = 10 - 3 = 7 "Odds against" is the ratio unfavorable : favorable \rightarrow 7:3	 Determine the fraction associated with chances of winning. Use those numbers to determine the values for favorable and unfavorable. Determine the ratio for the odds against.
Answer: The boxer's odds against winning are 7:3.	
Additional Resources:	1
Visions Volume 2, p. 153	

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Question:	General Strategies:
Sam bets \$12 on a horse race. The odds in favor of his horse winning are 4:5. How much money would Sam collect if his horse wins the race?	 Read the question. Highlight key words. Identify the math topic. Re-read the question. Make a prediction about the answer- what will it look like? (an equation, a number, etc.). Refer to your memory aid, as needed. Solve. Ask yourself whether your answer makes sense. Write your answer. Do not leave a blank!
Sam would collect \$ if his horse wins	My Strategies:

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Answer and Solution:	Suggested Strategies:
Answer and Solution: $\frac{4}{5} = \frac{12}{x}$ $x = 15 $$15 \text{ win + $12 bet } = 27 remittance	 Determine the proportion for calculating bets. Solve for the missing term. Don't forget the initial amount he bets. Don't forget the amount he initially bets.
Answer: Sam will receive \$27 if his horse wins.	
Visions Volume 2, p. 153	

A bag contains 20 marbles that are either blue or yellow.

If a marble is drawn at random from the bag, the odds that the marble will be blue are 1 to 4.

How many yellow marbles are in the bag?

General Strategies:

- 1. Read the question.
- 2. Highlight key words.
 3. Identify the math topic.
- 4. Re-read the question.
- Make a prediction about the answerwhat will it look like? (an equation, a number, etc.).
- 6. Refer to your memory aid, as needed.
- 7. Solve.
- 8. Ask yourself whether your answer makes sense.
- 9. Write your answer. Do not leave a blank!

My Strategies:

There are _____ yellow marbles in the bag.

Answer and Solution:

Odds for blue is the ratio favoring blue : against blue 1 : 4

The probability of drawing a blue marble is :

$$\frac{favoring \ blue}{total} = \frac{1}{1+4} = \frac{1}{5}$$

$$\frac{1}{5} = \frac{x}{20}$$

x = 4 blue marbles

20 - 4 = 16 yellow marbles

Suggested Strategies:

 Relate the given "odds" with a probability so that you can determine the number of blue marbles, and from there, the number of yellow marbles.

Answer: There are <u>16</u> yellow marbles in the bag.

Additional Resources:

Visions Volume 2, p. 153

6.3 Mathematical Expectation

Ques	tion:	Ge	neral Strategies:
Ques Ralph or hig Which A) B) C) D)	 tion: bets \$5 to play a game that involves rolling a die. If he rolls a 5 her, he receives \$10 plus his bet; otherwise, he loses his bet. a statement is true? The game is to the player's advantage. The game is fair. The game is to the player's disadvantage. The game's fairness cannot be determined. 	Ge 1. 2. 3. 4. 5. 6. 7. 8. 9. Do Ma My	neral Strategies: Read the question. Highlight key words. Identify the math topic. Re-read the question. Refer to your memory aid, as needed. Look carefully at each choice shown (A, then B, then C and then D). Eliminate options you know to be incorrect. Solve/check each possible choice. Select the choice that makes the most sense. not leave a blank! ke a choice!

Answer and Solution: Suggested Strategies: Expected value = $(P_1 \times O_1) + (P_2 \times O_2)$ • Find the probability of winning. $=\frac{2}{6}(10)+\frac{4}{6}(-5)=0$ • Find the probability of losing. • Find the profit you Because the expected value is 0, the game is fair. obtain from winning. • Find the profit you obtain from losing. • If the result is 0 then the game is fair. The answer is B. **Additional Resources:** Visions Volume 2, p. 164

Question:		General Strategies:		
A box	contains ten \$5 bills and fifteen \$10 bills.	1. Read the question.		
Players must bet \$8 in order to play the game.		 Aligning t key words. Identify the math 		
Players keep the bill they draw from the box.		4. Re-read the question.		
What is the expected gain of this game?		5. Refer to your memory aid, as needed.		
A)	-1	6. Solve the problem without looking at		
B)	0	C and D).		
C)	5	choices.		
D)	8	the appropriate choice.		
		Do not leave a blank! Make a choice!		
		My Strategies:		
Answer and Solution:	Suggested Strategies:			
---	---	--	--	--
Expected gain = $(P_1 \times 0_1) + (P_2 \times 0_2)$ = $\frac{10}{25}(5-8) + \frac{15}{25}(10-8) = 0$	 Find the probability of winning. Find the probability of losing. Find the profit you obtain from winning. 			
 A) -1 - if you mix up the probabilities B) 0 correct 	 Find the profit you obtain from losing. Calculate the expected gain. 			
C) 5 – if you mix up the probabilities and not consider the cost to play				
D) 8 – if you don't consider the cost to play				
Additional Resources:				
Visions Volume 2, p. 164				

Question:

A game involves throwing 2 coins.

If a player receives two heads, the player wins \$10.

If a player receives two tails, the player wins \$20.

If the player receives any other combination, the player loses \$5.

What is the expected value?

General Strategies:

- 1. Read the question.
- 2. Highlight key words.
- 3. Identify the math topic.
- 4. Re-read the question.
- Make a prediction about the answerwhat will it look like? (an equation, a number, etc.).
- 6. Refer to your memory aid, as needed.
- 7. Solve.
- 8. Ask yourself whether your answer makes sense.
- 9. Write your answer. Do not leave a blank!

My Strategies:

The expected value is ______.



Question:

It costs a smartphone manufacturer \$300 to make a phone. The phones they make are either sold to cell phone service companies for \$550 each, sold to retail stores for \$650 each, sold to employees for a special price of \$500 each, given away for promotional purposes or they turn out to be defective and have to be scrapped.

Over the past year, 50% of the phones were sold to cell phone service companies, 45.5% were sold to retail stores, 1% were sold to employees, 0.5% were given away, and 3% were defective and not sold.

The company plans on manufacturing one million phones next year.

What is the company's expected profit for next year?

General Strategies:

- 1. Read the question.
- 2. Highlight key words.
- Identify the math topic.
- 4. Re-read the question.
- Make a prediction about the answerwhat will it look like? (an equation, a number, etc.).
- 6. Refer to your memory aid, as needed.
- 7. Solve.
- Ask yourself whether your answer makes sense.
- 9. Write your answer. Do not leave a blank!

My Strategies:

The company's expected profit for next year is _

Answer and Solution:

outcome	cost	price	profit	probability	profit x probability
			<i>Oi</i>	Pi	$O_i \times P_i$
service company	\$300	\$550	\$250	50.0%	\$125
retail store	\$300	\$650	\$350	45.5%	\$159.25
employee	\$300	\$500	\$200	1.0%	\$2
give away	\$300	\$0	-\$300	0.5%	-\$1.5
defective	\$300	\$0	-\$300	3.0%	-\$9
total				100.0%	\$275.75

If there will be 1 000 000 phones produced, the expected profit would be $275.75 \times 1000000 = 275750000$.

OR

Expected Profit = $(P_1 \times 0_1) + (P_2 \times 0_2) + (P_3 \times 0_3) + (P_4 \times 0_4) + (P_5 \times 0_5)$ = $(0.5 \times 259) + (0.445 \times 350) + (0.01 \times 200) + (0.005 \times -300) + (0.03 \times -300)$ = 275.75 / phone x 1 x 10⁶ = 275 750 000

Suggested Strategies:

- These types of problems lend themselves very well to creating tables to keep track of all the subscripts in the formula.
- Identify outcomes not just what they are but the result (in this case, where the phones get sold determine the profit for those phones.)
- Identify probabilities of each outcome
- Remember that the formula would give you the expected value for one phone – don't forget to multiply by the number of phones.

The company's expected profit for next year is \$275 750 000.

Additional Resources:

Visions Volume 2, pp. 163-164

Question:

The Street Festival

Frank is creating a game for people to play at a street festival in the community.

His idea is to have a bag with 9 baseballs, each with a number written on it. The number will represent the dollar amount which will be won by the participant who randomly draws it out of the bag.

The participant pays \$3.00 to play the game.

Frank numbered the balls as shown below:



Sue is running the festival and insists that the game be fair or in favour of the participant.

Frank says his game meets that condition. Sue disagrees.

Who is correct?

□ Frank is correct.

□ Sue is correct.

General Strategies:

- 1. Read the problem.
- 2. Highlight key words.
- 3. Identify the math topics.
- 4. Re-read the problem.
- Define your steps (your game plan) – this is criteria 3.
- 6. Refer to your memory aid, as needed.
- 7. Solve.
- If you get stuck on a calculation, pick a number and keep going.
- Ask yourself whether your answer makes sense.
- 10. Write your answer statement.

Show any or all your work! Do not leave a blank page!

My Strategies:

Answer and Solution: There are 5 possible outcomes: Picking a ball with 1 on it – which means –2 gain Picking a ball with 2 on it – which means –1 gain Picking a ball with 3 on it - which means 0 gain Picking a ball with 5 on it – which means +2 gain Picking a ball with 6 on it – which means +3 gain ... because it costs \$3.00 to play The probability of each outcome is determined by how many of the 9 balls have that number on them. P(1) = 2/9 because there are 2 balls with a 1 P(2) = 2/9 because there are 2 balls with a 2 P(3) = 3/9 because there are 3 balls with a 3 P(5) = 1/9 because there is 1 ball with a 5 P(6) = 1/9 because there is 1 ball with a 6 $P_1 \times (O_1) + P_2 \times (O_2) + \dots = expected value$ $P(1) \times (-2) + P(2) \times (-1) + P(3) \times (0) + P(5) \times (2) + P(6) \times (3) = EV$ $\frac{2}{9} \times (-2) + \frac{2}{9} \times (-1) + \frac{3}{9} \times (0) + \frac{1}{9} \times (2) + \frac{1}{9} \times (3) = EV$ $\frac{-4}{9} + \frac{-2}{9} + \frac{0}{9} + \frac{2}{9} + \frac{3}{9} = EV$ $\frac{-4}{9} + \frac{-2}{9} + \frac{0}{9} + \frac{2}{9} + \frac{3}{9} = EV$ $\frac{-1}{9} = EV$ probability outcome gain x probability gain

Number on the ball	<i>O</i> _i	P _i	<i>O_i</i> x <i>P_i</i>	
1	-\$2	2/9	-4/9	
2	-\$1	2/9	-2/9	
3	\$0	3/9	0/9	
5	\$2	1/9	2/9	
6	\$3	1/9	3/9	
total		9/9	-1/9	

Conclusion: since the expected value is negative, this game is not in the participant's favour.

□ Frank is correct.

Sue is correct.

Additional Resources:

Visions Volume 2, pp. 163-164

Suggested Strategies:

Some of the key words:

- Game
- Random
- Fair
- **Buying tickets**
- Won

This is an expected value question.

What you need:

- All the possible outcomes
- The probability of each outcome

Things to check:

- Make sure all your probabilities add up to 1
- Make sure you have one term for each outcome (in this case 5)
- Make sure some of your terms are negative and some are positive
- Make sure you come to the correct conclusion; a "negative gain" is a "loss"
- You can also set up your solution in a table.

Note, that you can 'guess' this answer by checking one of the boxes, but you won't get credit for the guess - you have to show your reasoning in order to get marks.